

# Application of atomistic force field potentials for the prediction of heat transport and phonon properties in metal-organic frameworks

Sandro Wieser

Institute of Solid-State Physics

DocDay of the Doctoral School Physics

02.02.2023

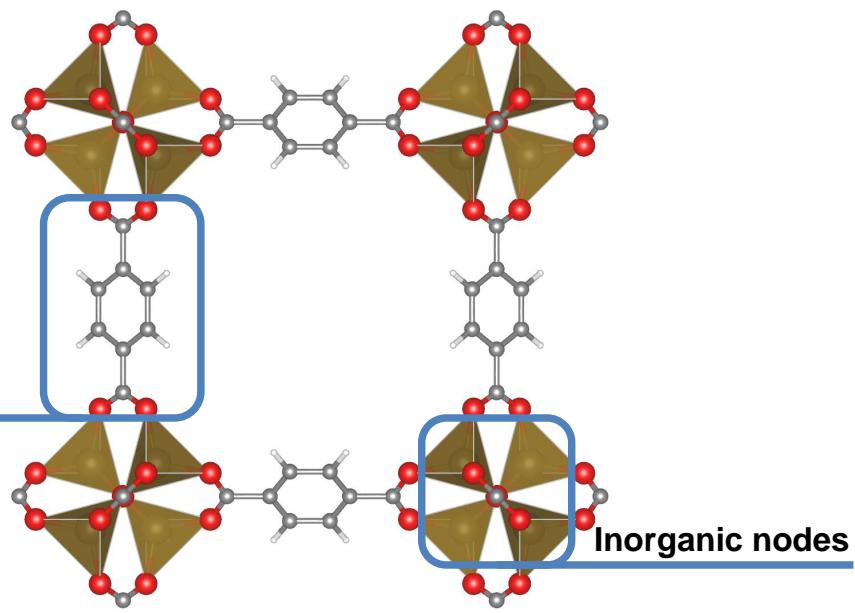
Special thanks to Egbert Zojer, Tomas Kamencek, Natalia Bedoya-Martínez (MCL Leoben), the Schmid group from the Ruhr Universität Bochum, and the Advanced Materials Modeling group at the Institute of Solid-State Physics

sandro.wieser@tugraz.at

## Metal-Organic Frameworks (MOFs)

● Zn  
● O  
● C  
○ H

Organic Linkers



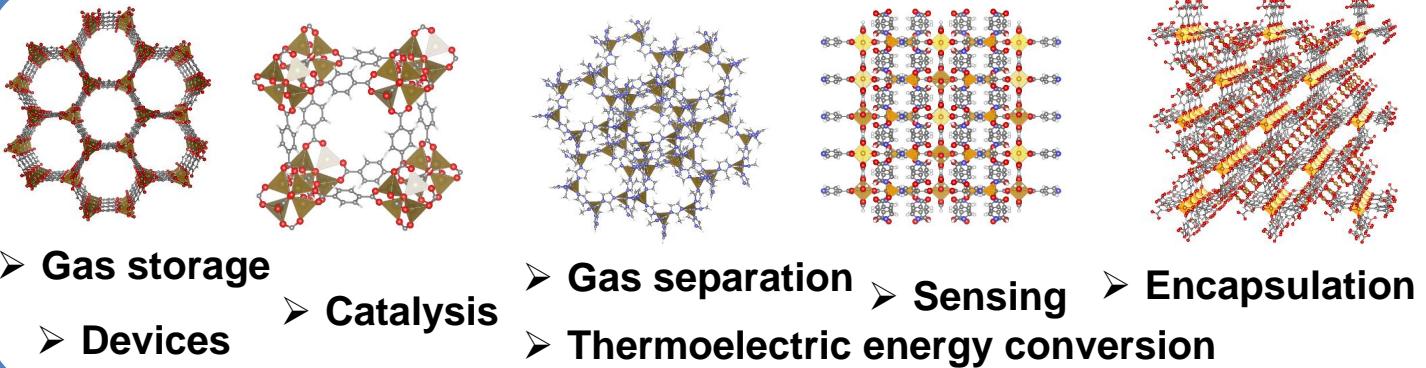
Inorganic nodes

**Isoreticular MOF-1 (IRMOF-I)**

sandro.wieser@tugraz.at

## 3 Why are we interested in phononic heat transport in MOFs?

3

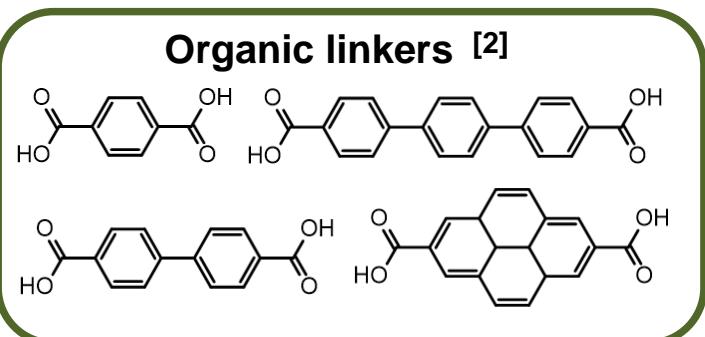
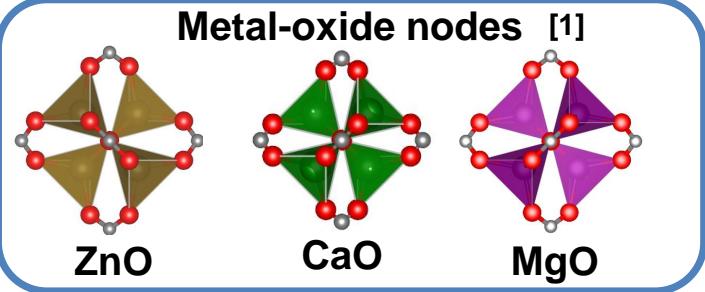
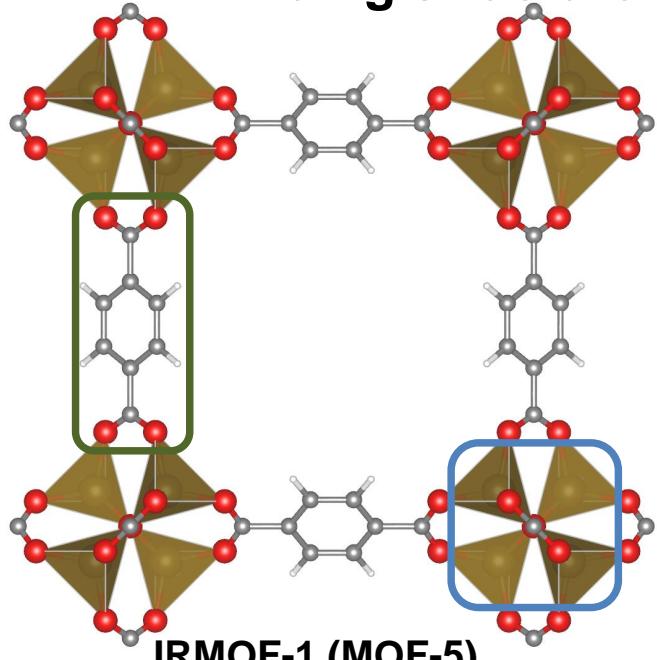


Many processes during applications **generate heat**  
→ **Heat dissipation** often is a limiting factor!

Usually poor electrical conductors → Phononic heat transport

4

## Understanding heat transport: finding structure to property relationships

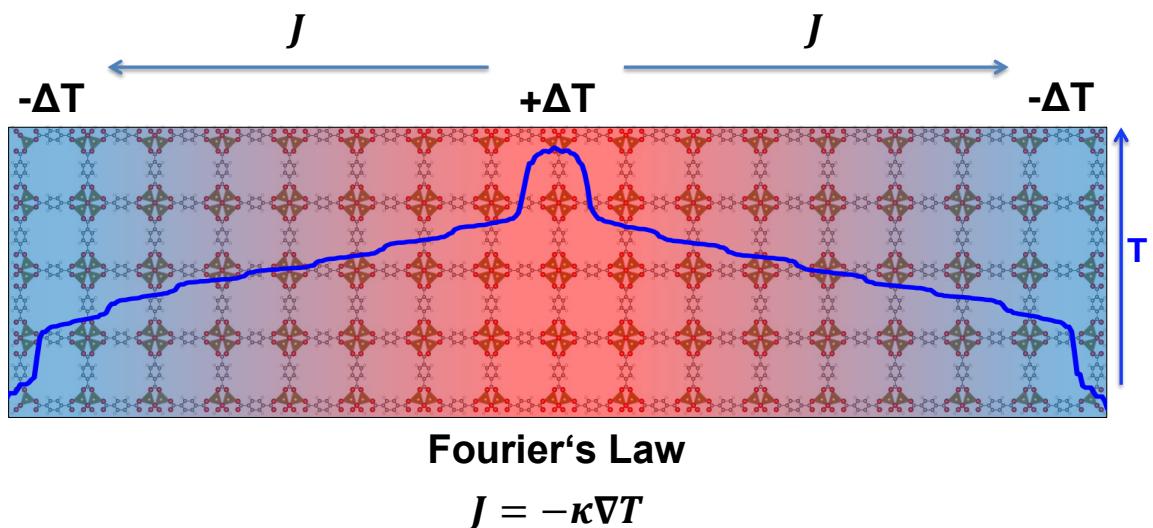


[1] S. Wieser et al., *Adv. Theory Simulations* **2020**, 2000211.

[2] S. Wieser et al., *Nanomaterials* **2022**, 12, 2142.

sandro.wieser@tugraz.at

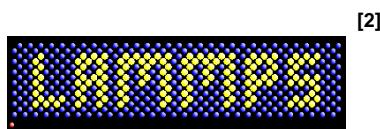
## Non-Equilibrium Molecular Dynamics (NEMD)



## Non-Equilibrium Molecular Dynamics (NEMD)

Require simulation times over several **ns** with **fs** timesteps involving thousands of atoms

→ System specific classical Force-fields:  
MOF-FF<sup>[1]</sup> parameterized on ab-initio reference data

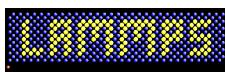


[1]: S. Bureekaew et al., *Phys. Status Solidi Basic Res.* **2013**, 250, 1128.

[2]: A. P. Thompson et al., *Comput. Phys. Commun.* **2022**, 271, 108171.

## Non-Equilibrium Molecular Dynamics (NEMD)

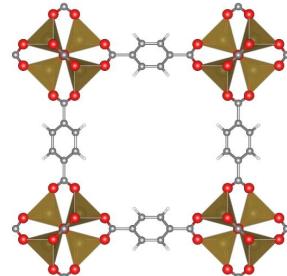
Require simulation times over several **ns** with **fs timesteps**  
involving thousands of atoms

<sup>[2]</sup>

→ System specific classical Force-fields:

MOF-FF<sup>[1]</sup> parameterized on ab-initio reference data  
transferable force-fields often fail!

Method	finite size corrected thermal cond. / W/(mK)
experimental <sup>[3]</sup>	0.32
MOF-FF	0.29
Dreiding	1.10
UFF4MOF	0.85



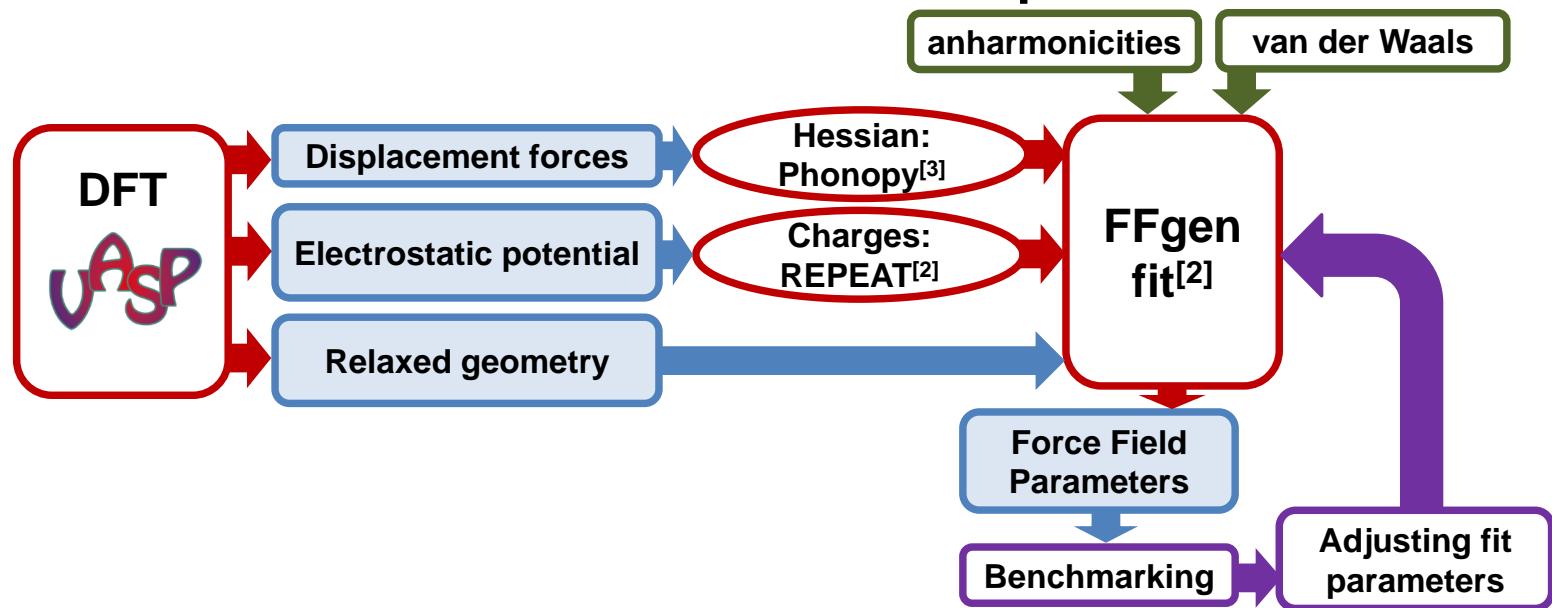
[3]: B.L. Huang et al. *Int. J. Heat Mass Transf.* **2007**, 50, 405–411

[1]: S. Bureekaew et al., *Phys. Status Solidi Basic Res.* **2013**, 250, 1128.

[2]: A. P. Thompson et al., *Comput. Phys. Commun.* **2022**, 271, 108171.

sandro.wieser@tugraz.at

## Parameterization of MOF-FF potentials

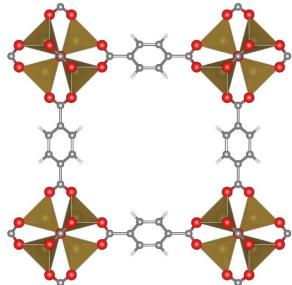


[1]: Bureekaew, S. et al. (2013). *Physica Status Solidi (B)*, 250(6), 1128–1141; Dürholt, J. P. et al. (2019). *JCTC*, 15(4), 2420–2432.

[2]: Campañá, C. et al. *J. Chem. Theory Comput.* 2009, 5, 2866–2878.

[3]: Togo, A. et al. *Scr. Mater.* 2015, 108, 1–5.

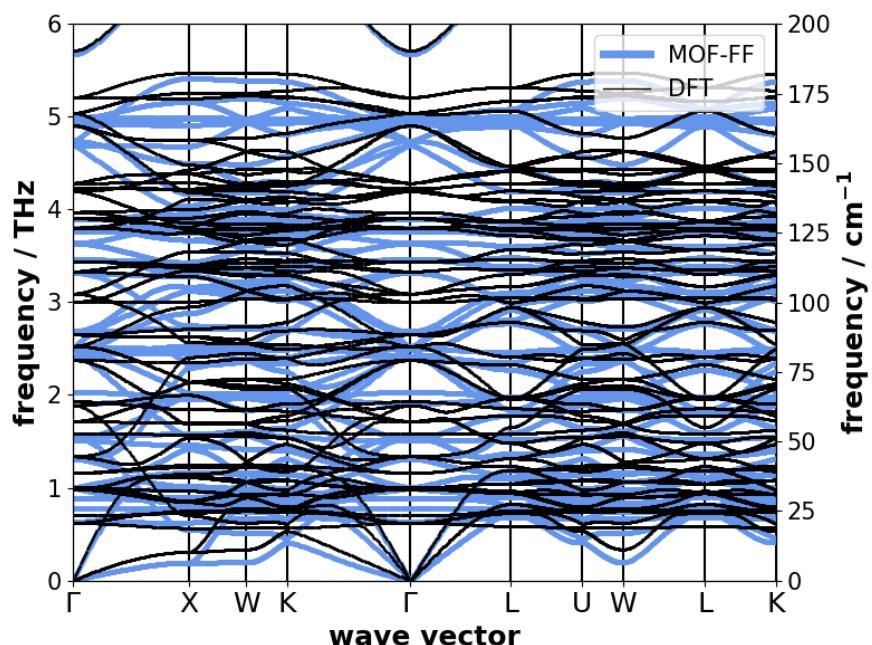
## Validation of the force field potential



**Phonon band structure of IRMOF-1**

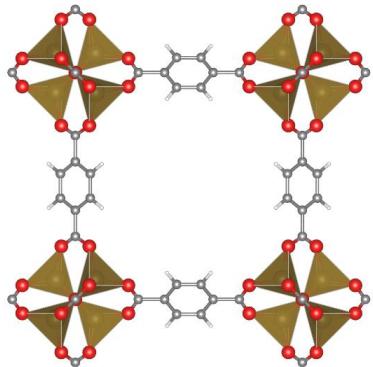
**Also benchmarked:**

- forces
- geometry of structure
- thermal expansion

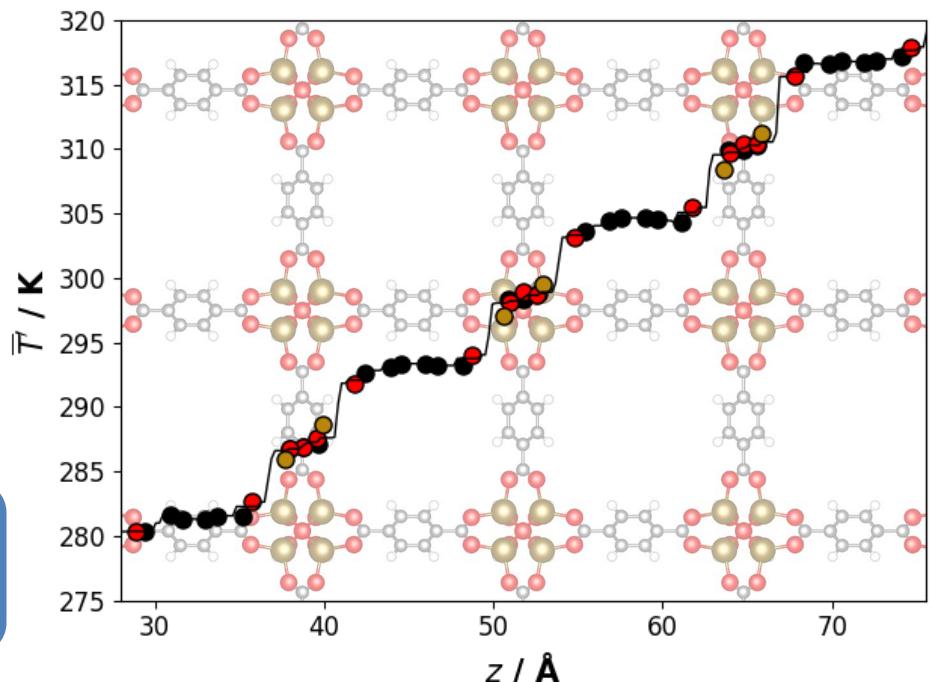


## Temperature profiles

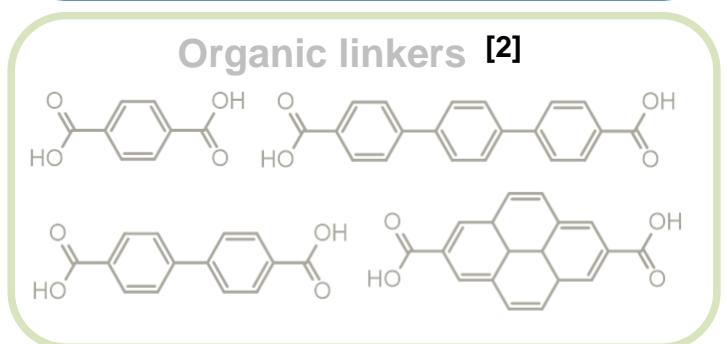
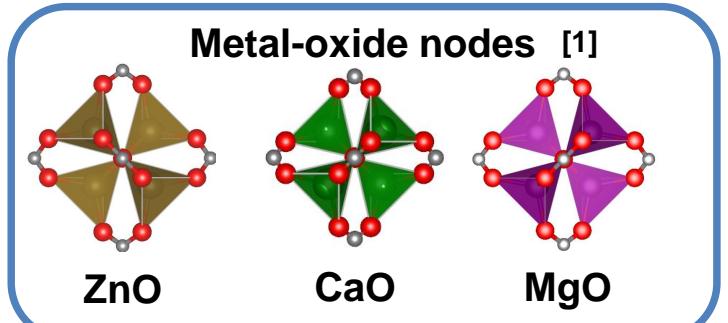
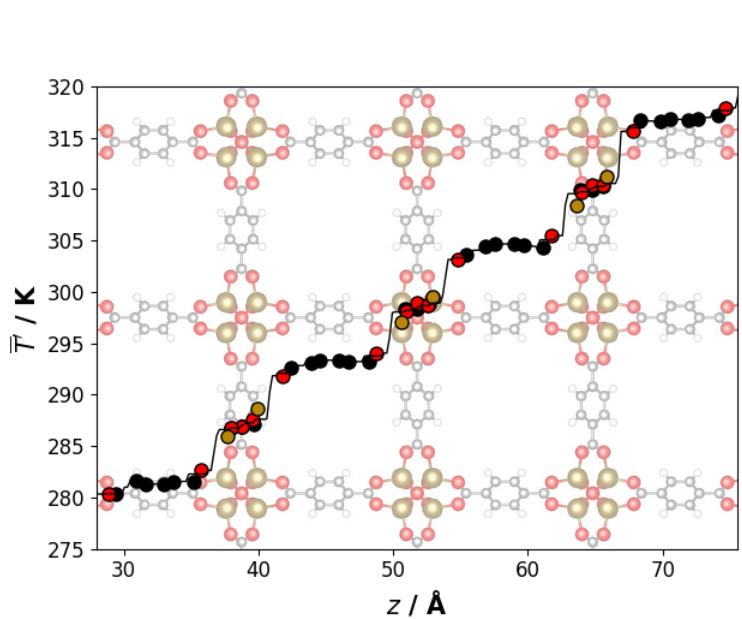
**IRMOF-1 (Zn)**



**Linker/Node interface:  
heat transport  
bottleneck**



## The impact of the node metal

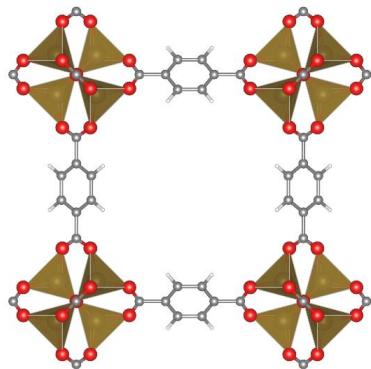


[1] S. Wieser et al., *Adv. Theory Simulations* **2020**, 2000211, DOI 10.1002/adts.202000211.

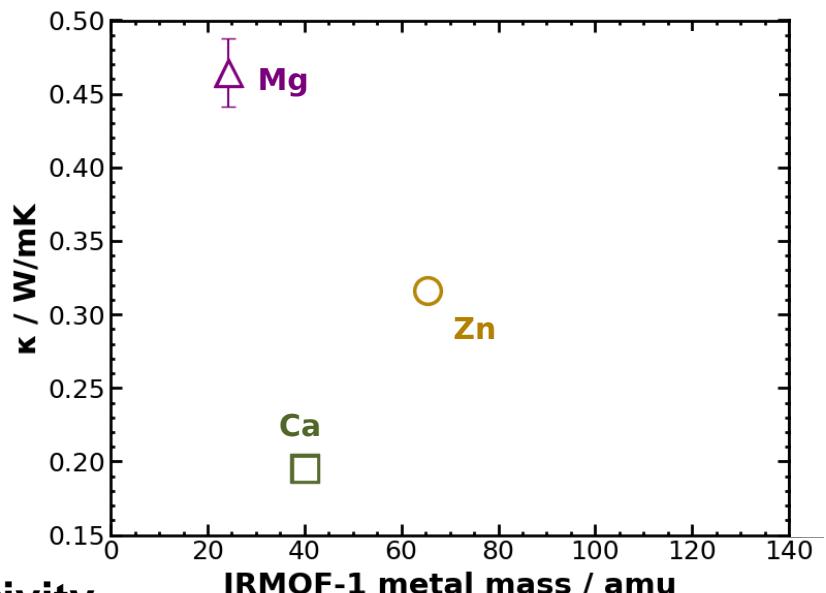
[2] S. Wieser et al., *Nanomaterials* **2022**, 12, 2142.

sandro.wieser@tugraz.at

## Thermal conductivities for investigated MOFs at 300K



**Expectation:**  
**lower metal mass:**  
**→ higher thermal conductivity**

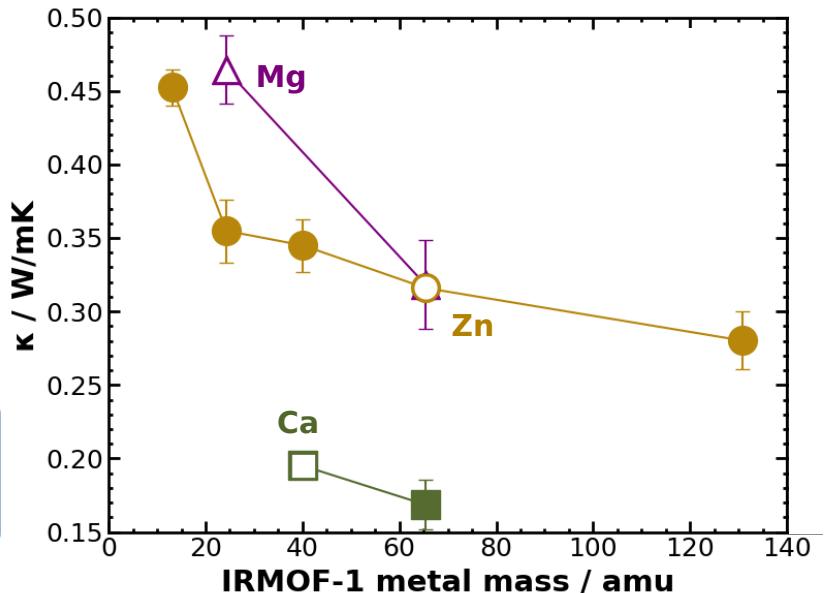


## Thermal conductivities for investigated MOFs at 300K

**Scaling of metal masses:**

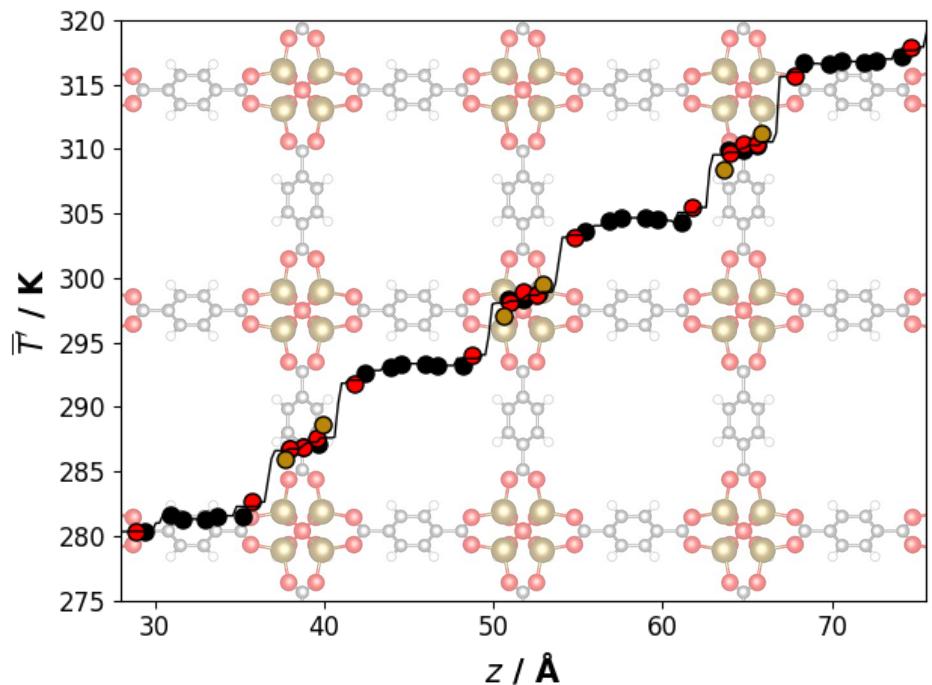
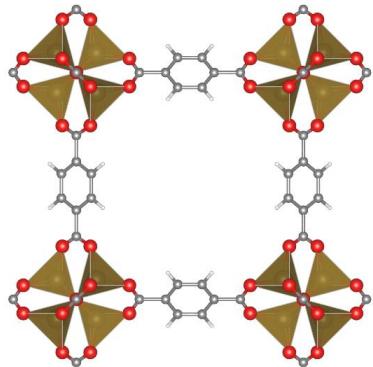
- Hypothetical systems
- Real systems

→ The difference in mass does not explain the low thermal conductivity for Ca



## Temperature profiles

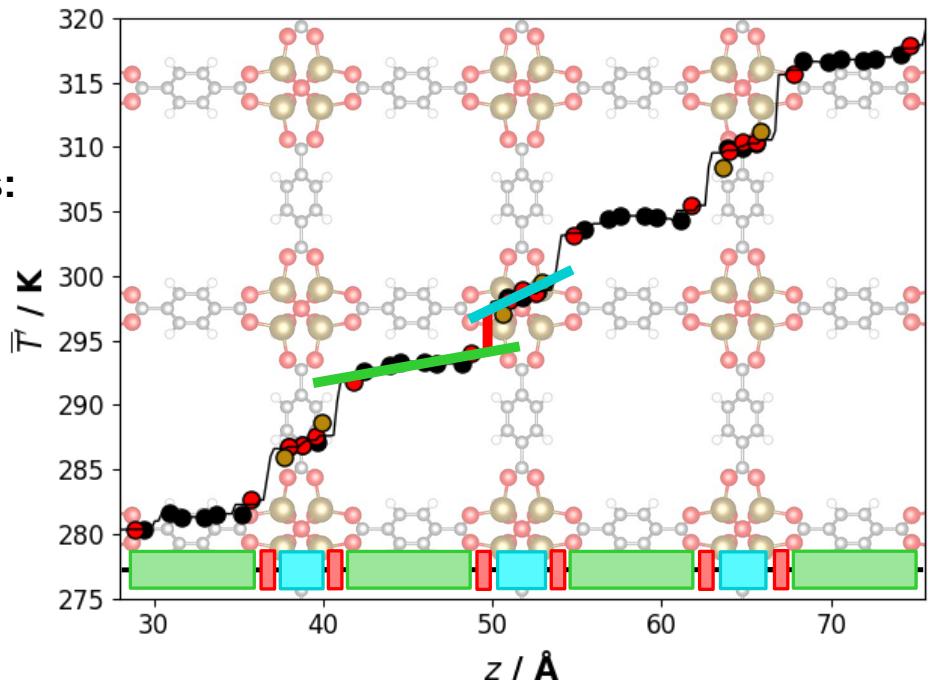
**IRMOF-1 (Zn)**



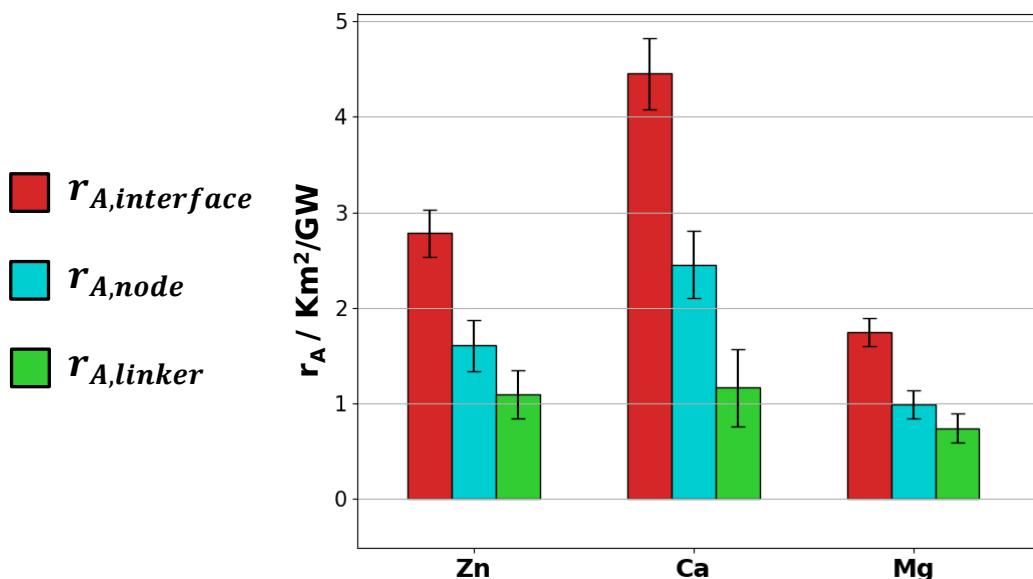
## Temperature profiles

**Model for thermal resistance contributions:**

$$r_{A,\text{unit}} = r_{A,\text{node}} + r_{A,\text{linker}} + 2 \cdot r_{A,\text{interface}}$$



## Contributions toward the thermal resistance



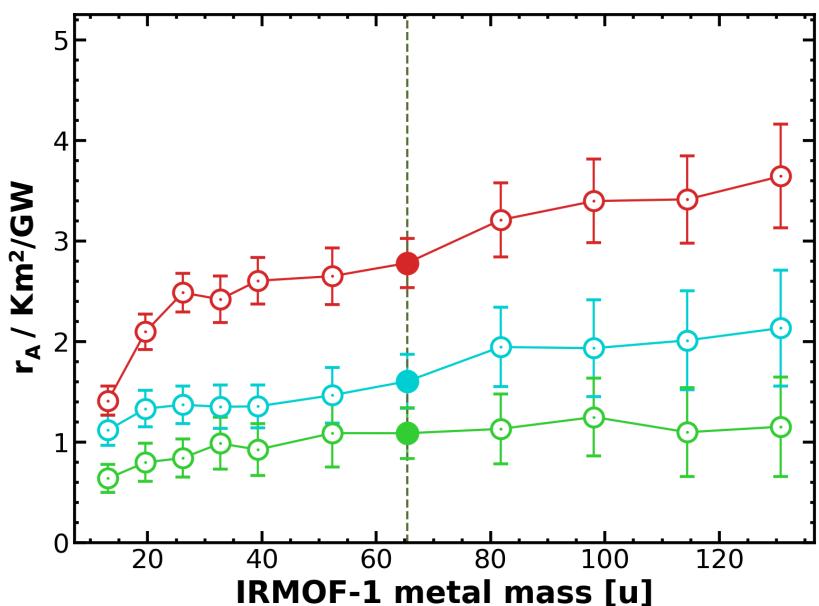
→ The interface shows the largest thermal resistance contribution

## Effect of the metal mass: IRMOF-I (Zn)

Scaling of metal masses:

- Hypothetical systems
- Real systems

- $r_{A,interface}$
- $r_{A,node}$
- $r_{A,linker}$



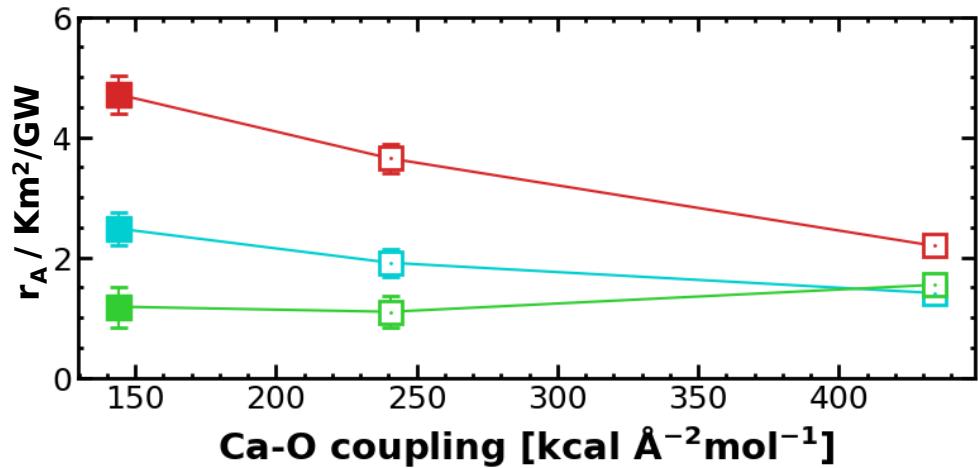
→ Lower metal mass reduces interface resistance

## Effect of node-linker interaction strength: IRMOF-I (Ca)

Scaling of metal masses:

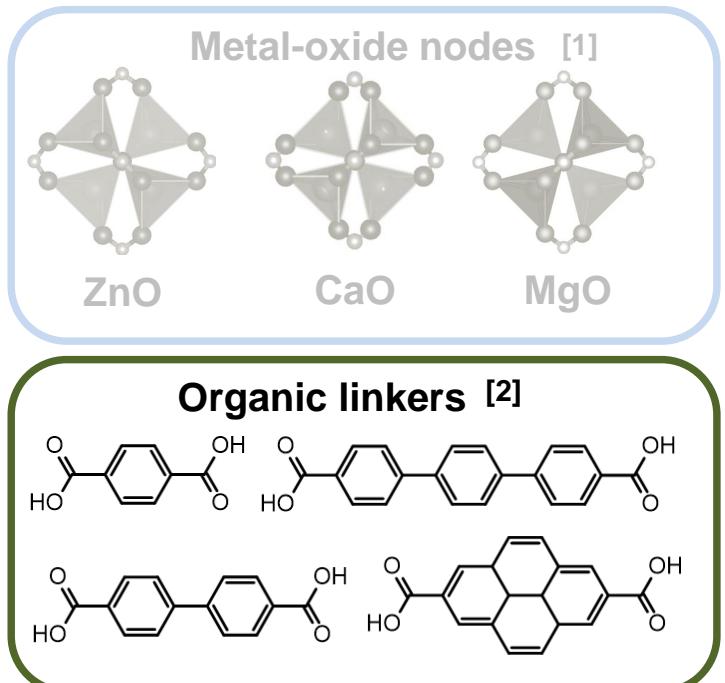
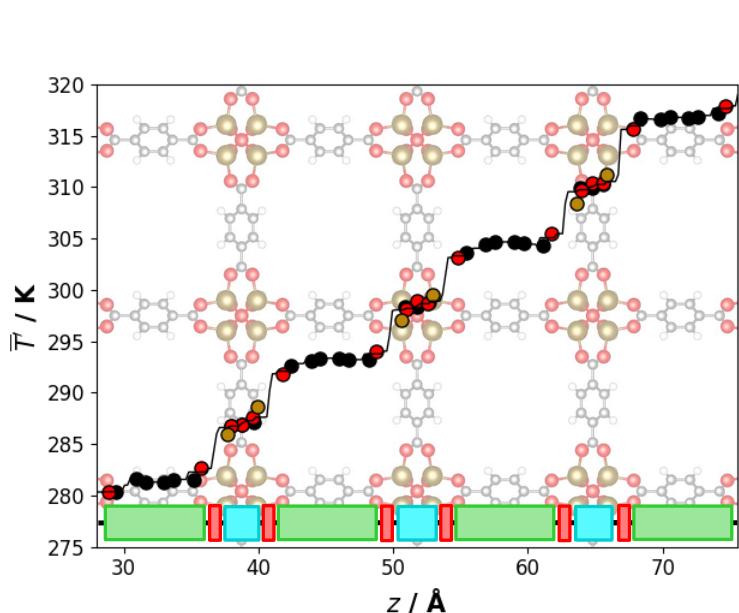
- Hypothetical systems
- Real systems

- $r_{A,\text{interface}}$
- $r_{A,\text{node}}$
- $r_{A,\text{linker}}$



→ Higher coupling strength reduces interface resistance

## The impact of the organic linker



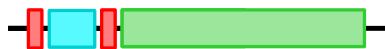
[1] S. Wieser et al., *Adv. Theory Simulations* **2020**, 2000211, DOI 10.1002/adts.202000211.

[2] S. Wieser et al., *Nanomaterials* **2022**, 12, 2142.

sandro.wieser@tugraz.at

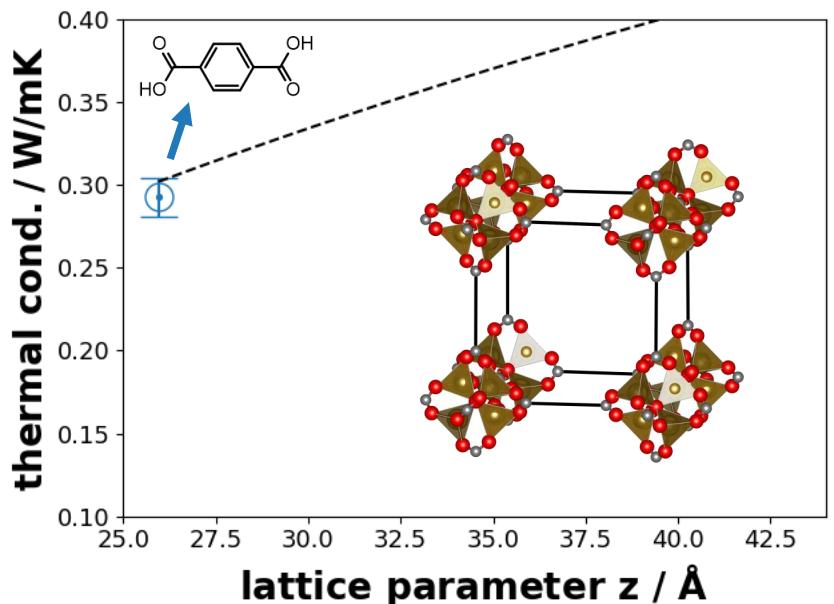
## Effect of linker length

**Model for thermal resistance contributions:**



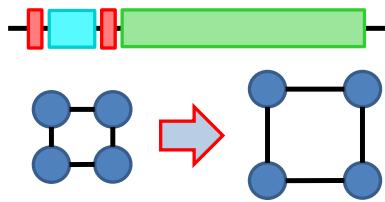
$$r_{A,\text{unit}} = r_{A,\text{node}} + r_{A,\text{linker}} + 2 \cdot r_{A,\text{interface}}$$

**Assumptions:**  
 ----- reduce interface density



## Effect of linker length

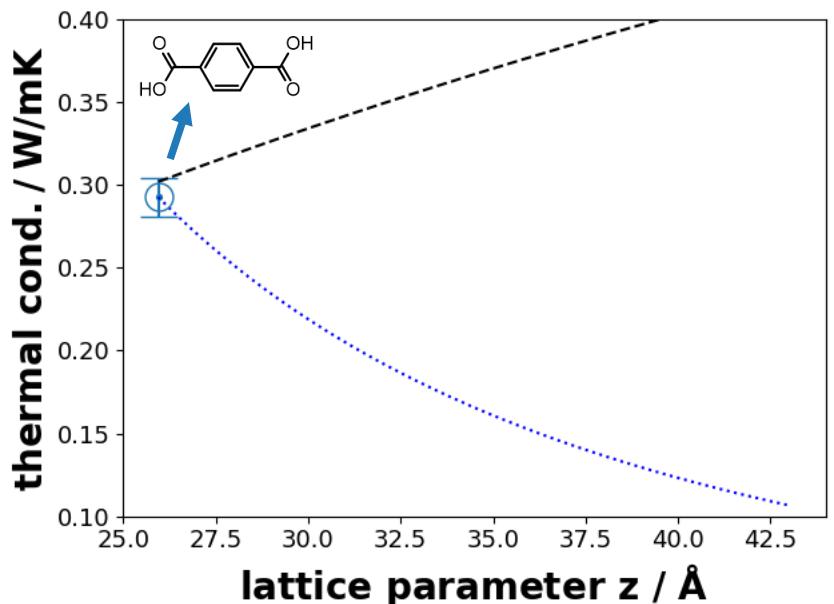
**Model for thermal resistance contributions:**



**Assumptions:**

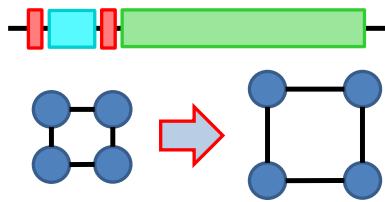
----- reduce interface density

..... heat transport  $\sim 1/A_{\text{cross}}$



## Effect of linker length

**Model for thermal resistance contributions:**

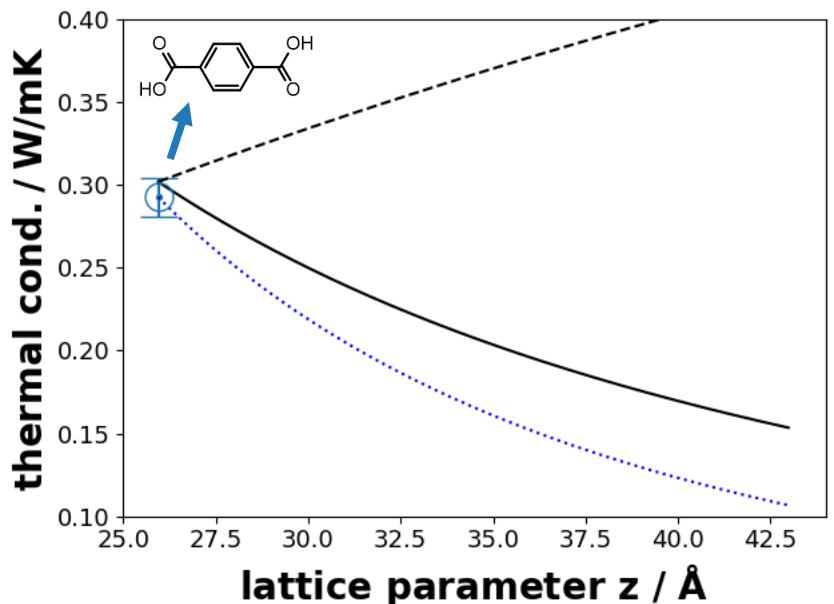


**Assumptions:**

----- reduce interface density

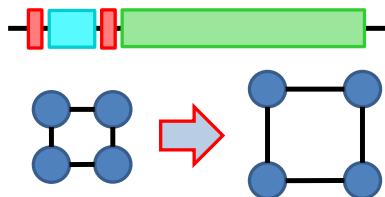
..... heat transport  $\sim 1/A_{\text{cross}}$

— combined effect



## Effect of linker length

**Model for thermal resistance contributions:**

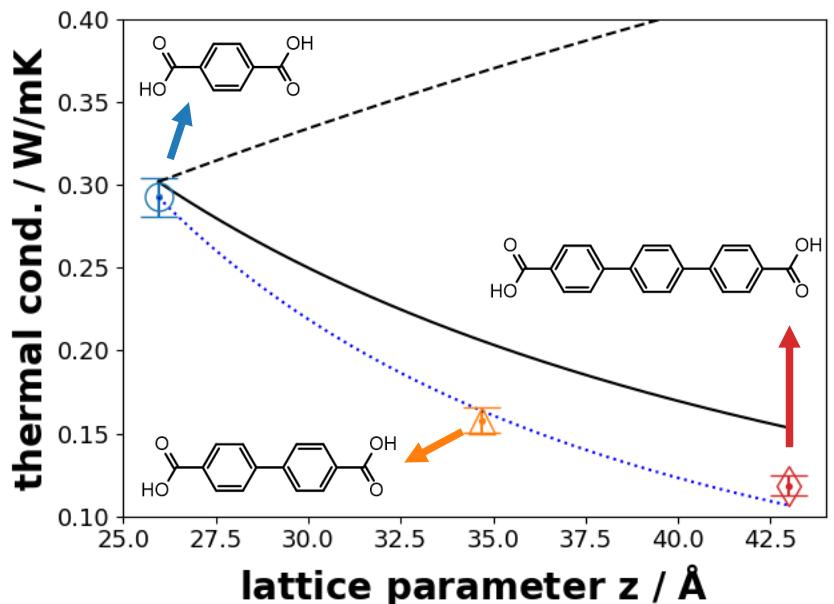


**Assumptions:**

----- reduce interface density

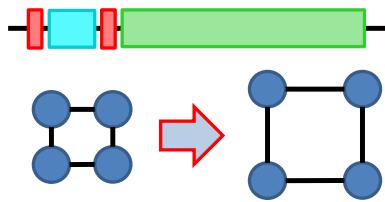
..... heat transport  $\sim 1/A_{\text{cross}}$

— combined effect



## Effect of linker length

**Model for thermal resistance contributions:**

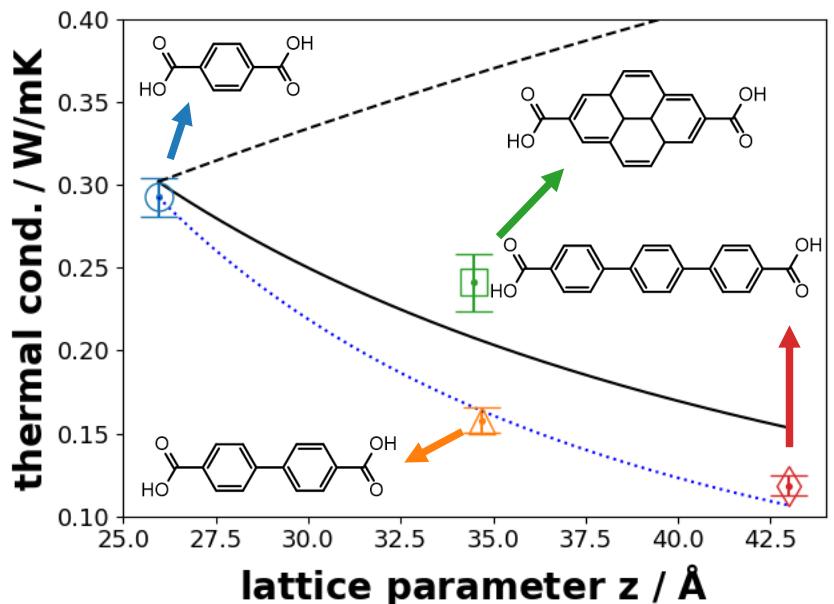


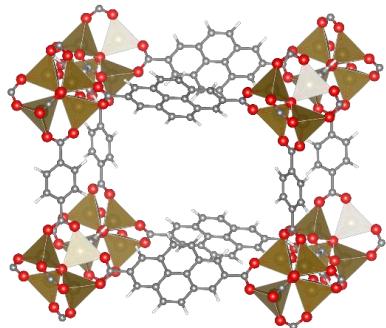
**Assumptions:**

----- reduce interface density

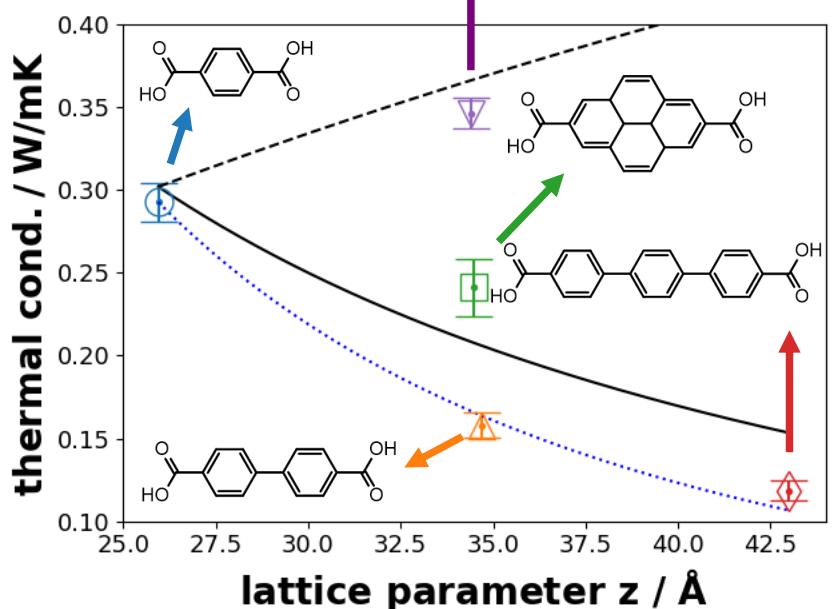
..... heat transport  $\sim 1/A_{\text{cross}}$

— combined effect





## Effect of linker length



### Assumptions:

----- reduce interface density

..... heat transport  $\sim 1/A_{\text{cross}}$

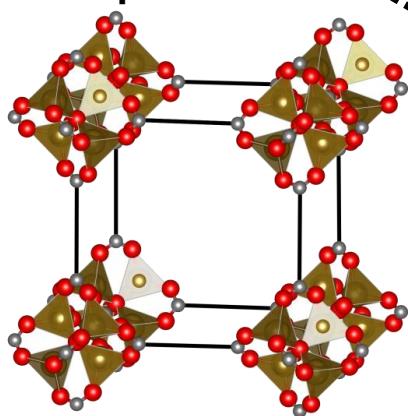
— combined effect

 interface

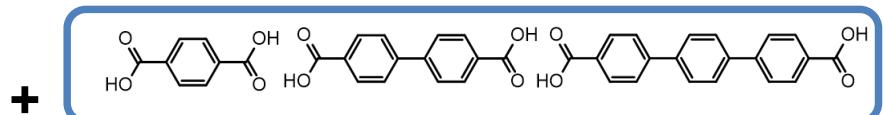
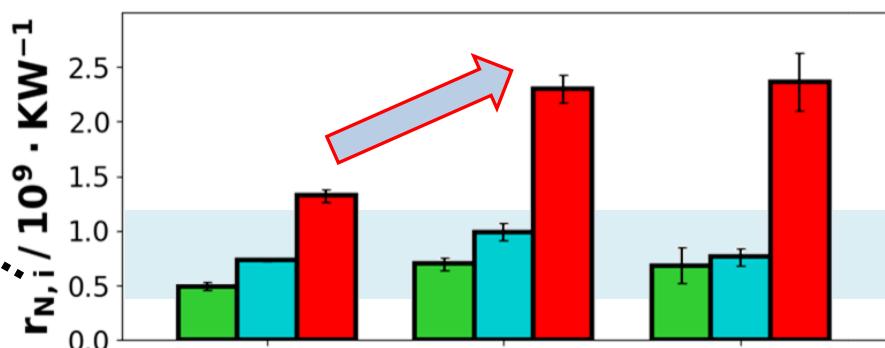
 node

 linker

for each heat transport channel

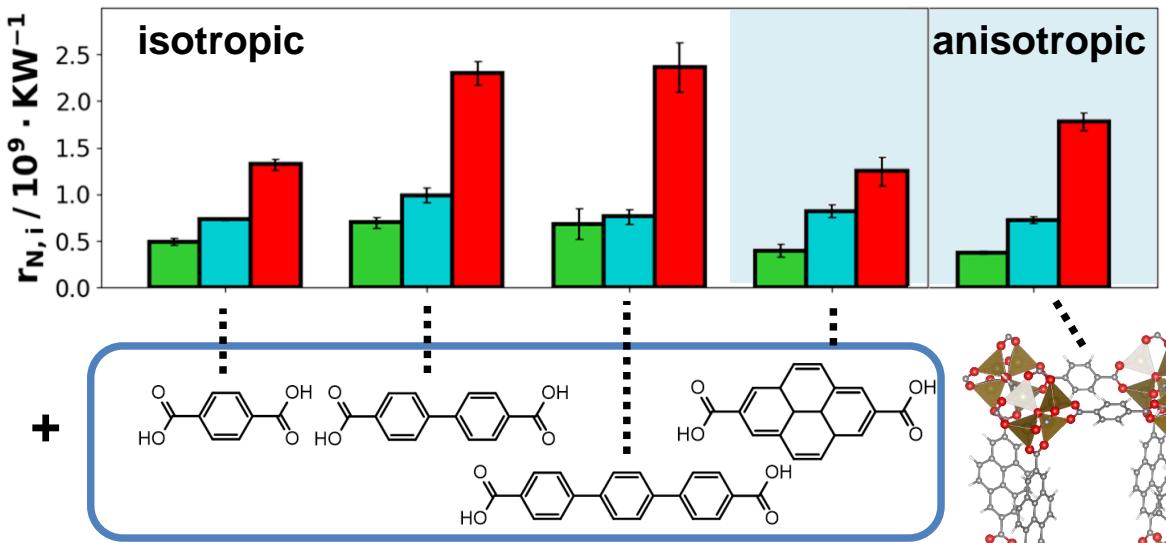
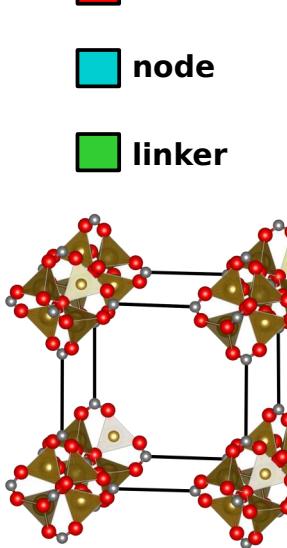


## Thermal resistance contributions

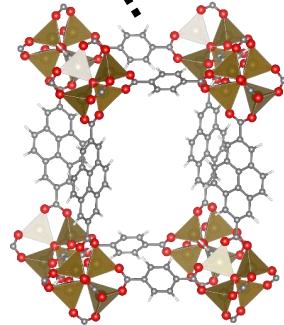


→ Longer linkers lead to higher interface resistance

## Thermal resistance contributions



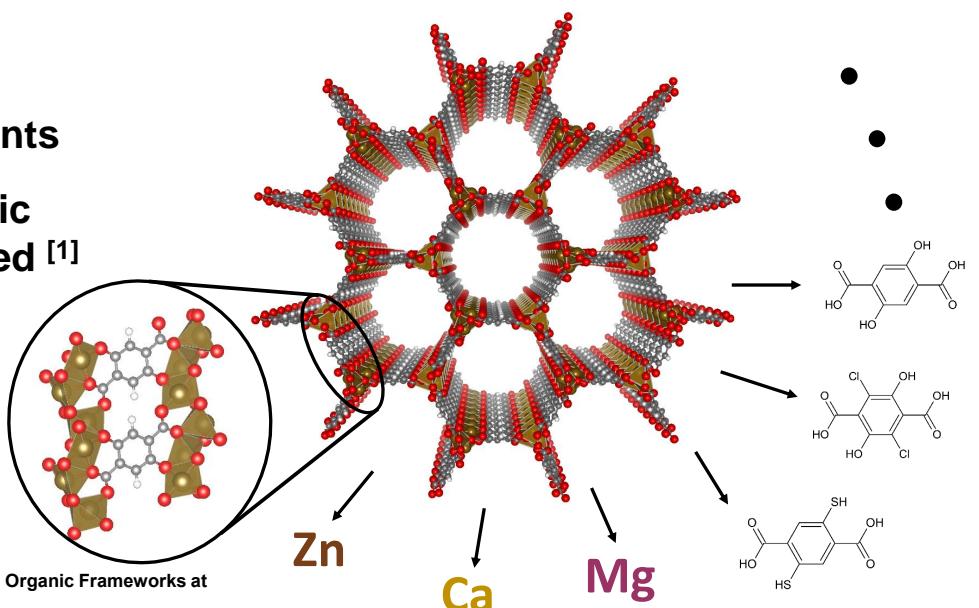
→ Longer linkers lead to higher interface resistance  
 → Pyrene linkers do not show this increase



## Investigating different materials: Example of MOF-74

**Structure dependent heat transport in MOF-74 variants**

**Large differences in elastic properties already reported [1]**



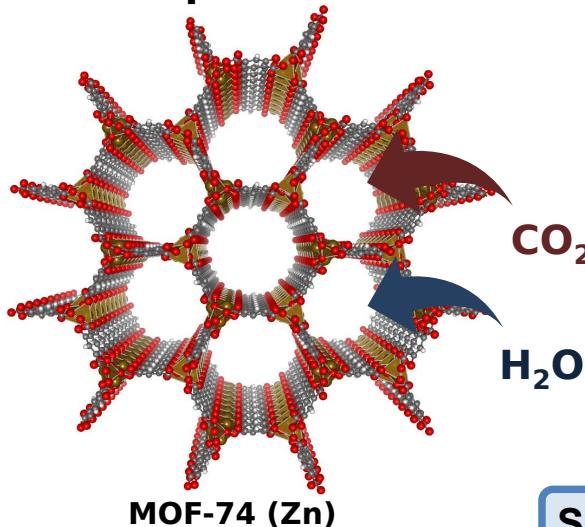
[1] Kamencsek, T.; Zojer, E.

Understanding the Anisotropic Elastic Properties of Metal – Organic Frameworks at the Nanoscale : The Instructive Example of MOF-74.

Journal of Physical Chemistry, 2021

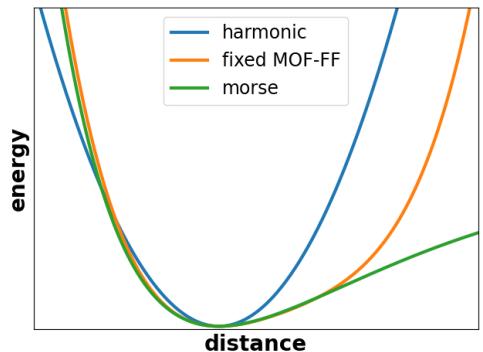
## The problems with the force field creation approach: The example of MOF-74

➤ complex MOFs



➤ human resource intensive

➤ Anharmonic contributions



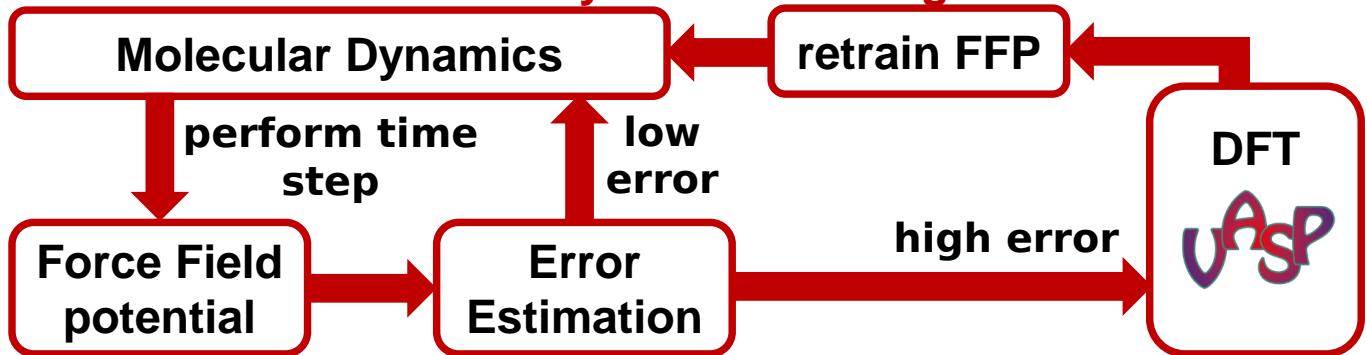
**SOLUTION: machine learning potentials**

## Machine learned potentials

- requires little human input
- capable of interpolating well within the reference data set

**How to properly obtain representative reference data sets?**

**On-the-fly Active learning<sup>[1]</sup>**



[1] R. Jinnouchi, F. Karsai, G. Kresse, *Phys. Rev. B* 2019

## Moment Tensor Potentials

- VASP potential can be learned fast, but: too slow for NEMD
- Solution: Moment tensor potentials (MTPs)<sup>[1]</sup> trained on the VASP sampled reference data

$$E(\text{cfg}) = \sum V_{\text{atom},i}(\text{neighborhood})$$



**VASP**  
 dynamic basis set based on local configurations

**MTP**  
 fixed basis set based on physically motivated interactions

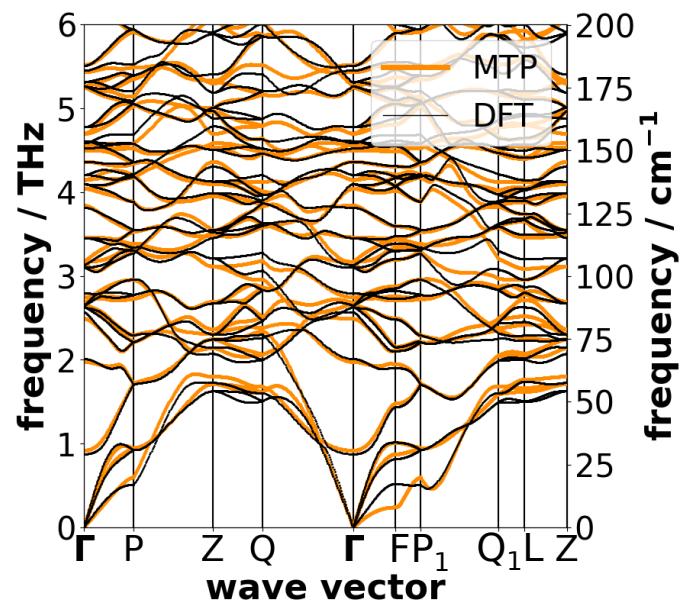
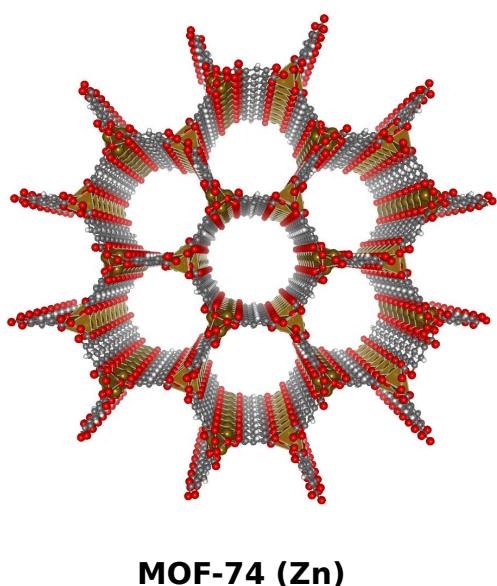
### Advantages:

- faster
- easy precision/speed adjustment
- increased accuracy

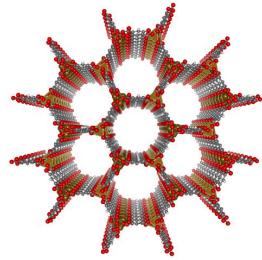
[1] A. V Shapeev, *Multiscale Model. Simul.* **2016**, *14*, 1153.

sandro.wieser@tugraz.at

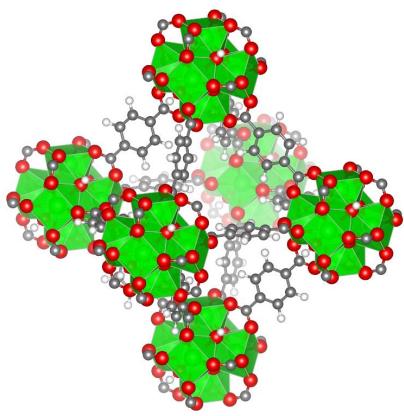
## Agreement of phonon frequencies



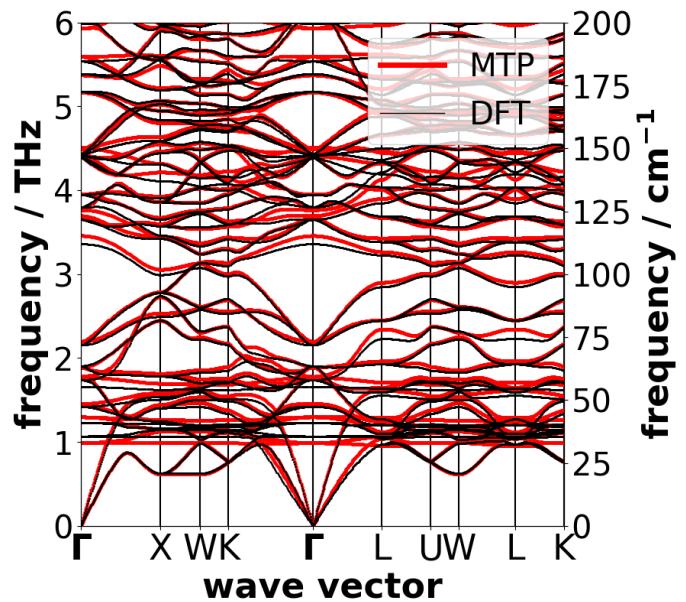
## Agreement of phonon properties



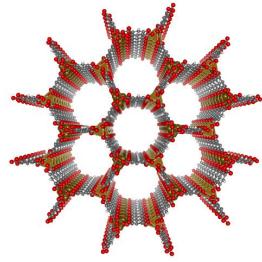
MOF-74 (Zn)



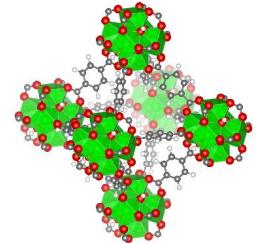
UiO-66 (Zr)



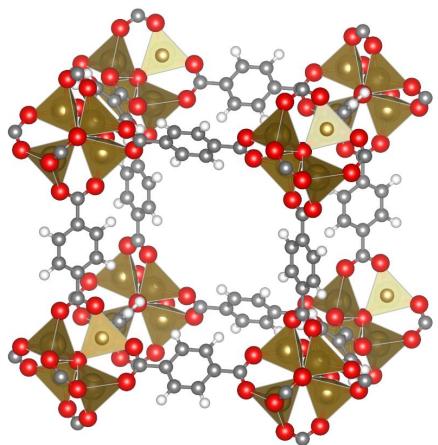
## Agreement of phonon properties



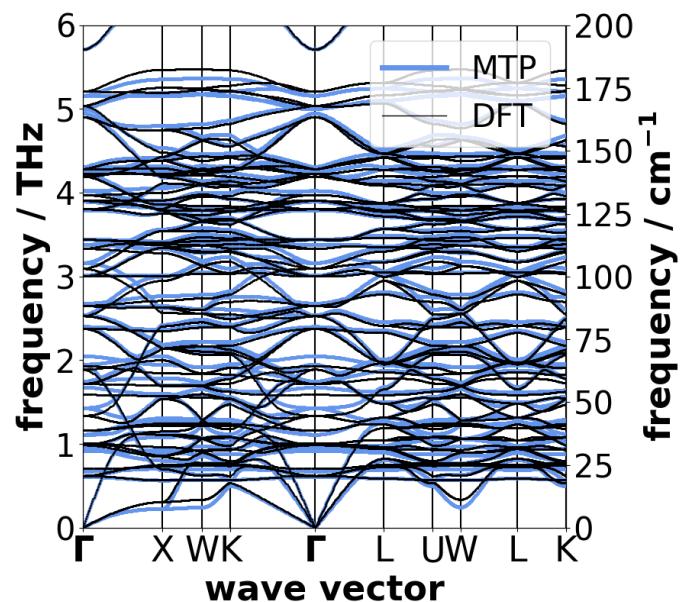
MOF-74 (Zn)



UiO-66 (Zr)

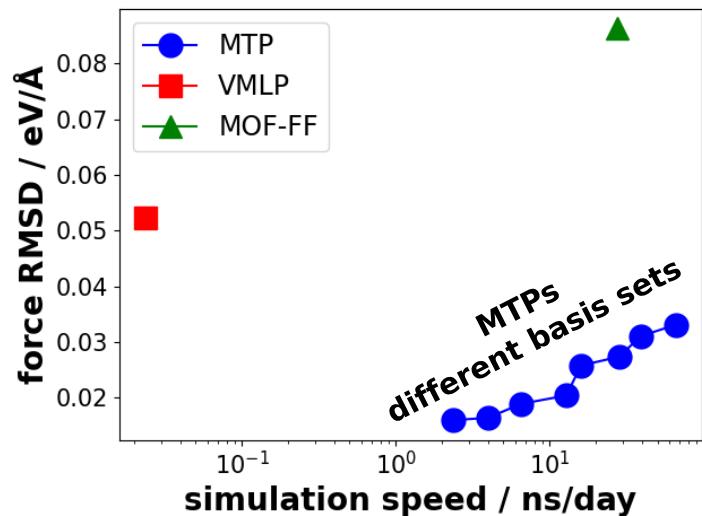
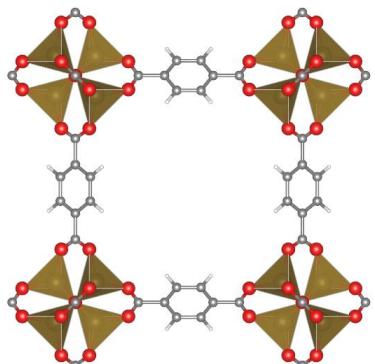


IRMOF-1 (Zn)



## Comparison of computational speed and accuracy

**IRMOF-1 (Zn)**



➤ Computation of the thermal conductivity feasible

Result at 300 K: 0.33 W/mK compared to experiment<sup>[1]</sup>: 0.32 W/mK

[1]: B.L. Huang et al. *Int. J. Heat Mass Transf.* 2007, 50, 405–411

sandro.wieser@tugraz.at

## Conclusion

- Node-Linker interface represents the most significant barrier for heat transport
- Lower metal masses and stronger metal-oxygen interaction strengths increase the thermal conductivity.
- Longer linker length reduces the thermal conductivity primarily due to pore size but also due to an increase in interface resistance
- Emerging Machine learning potential approaches offer an excellent tool to accurately describe phonon properties even in complex materials such as MOFs



—  
**ÖAW**  
—  
Grant No. 26163



Lead Project (LP-03):  
Porous Materials @Work

