



# In-situ test for Large Solar Thermal Collector Arrays

Results from the MeQuSo project

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# Collector Arrays at FHW

FHW = Fernheizwerk Graz

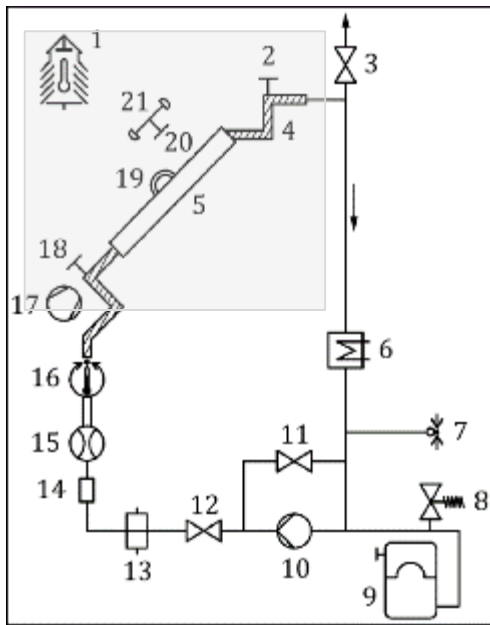


Source: Picfly.at Thomas Eberhard

# Test Methods for Solar Thermal Collectors

## Single collectors

- standard laboratory tests
- Solar Keymark, ISO 9806



Source: ISO 9806:2013

## Collector arrays

- no standard tests available
- higher system complexity; in-situ tests required



**D-CAT method**  
Project MeQuSo

## ▪ D-CAT: collector array test method

- Data-driven & model-based condition monitoring
- In-situ = system size vs. lab size
- Don't impair system operation

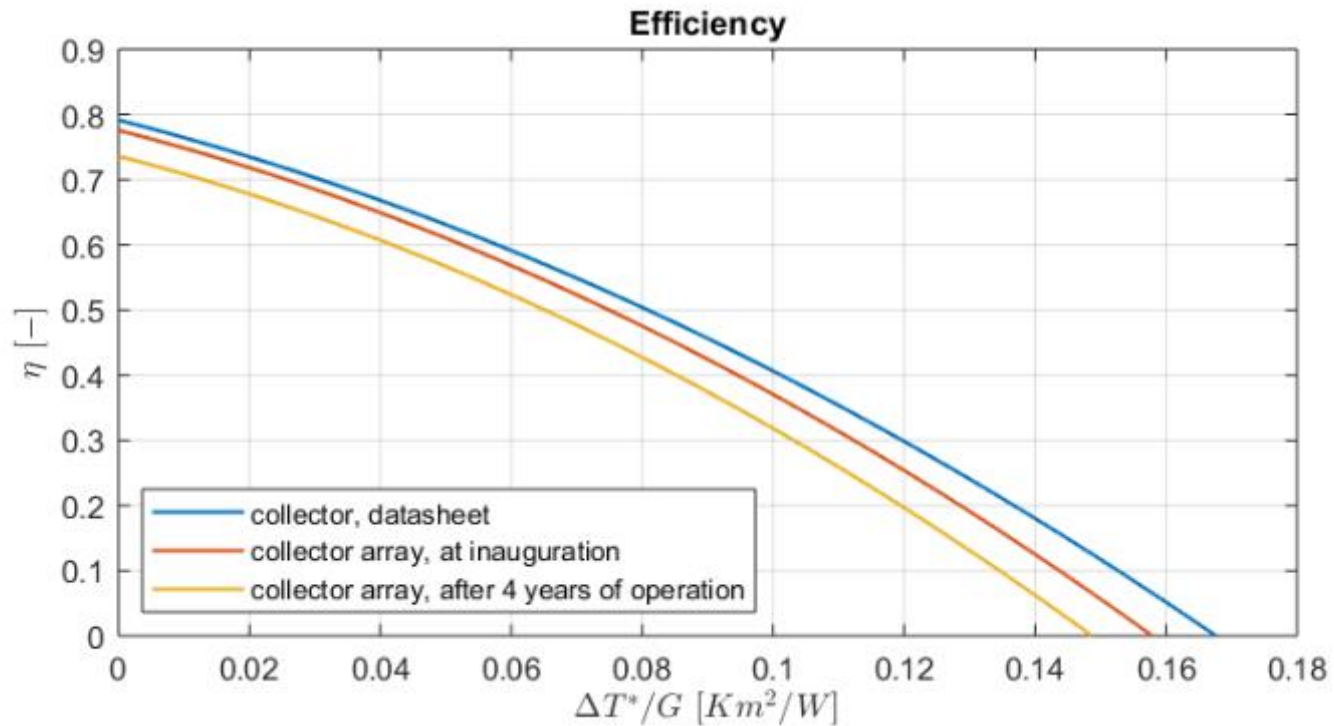
Performance parameters related to aperture area		$\eta_0$	a1	a2						
Units		-	W/(m <sup>2</sup> K)	W/(m <sup>2</sup> K <sup>2</sup> )						
Test results - Flow rate and fluid see note 1		0.769	2.67	0.009						
Bi-directional incidence angle modifiers?	No	<i>K<math>\theta</math> values are obligatory for 50°.</i>								
Incidence angle modifiers K $\theta$ ( $\theta$ )	Angle	10°	20°	30°	40°	50°	60°	70°	80°	90°
	K $\theta$ ( $\theta$ )	1.00	0.99	0.98	0.95	0.91	0.84	0.69	0.24	0.00
Incidence angle modifier not bi-directional - leave fields blank										





# D-CAT: Automated System Tests

Exemplary result



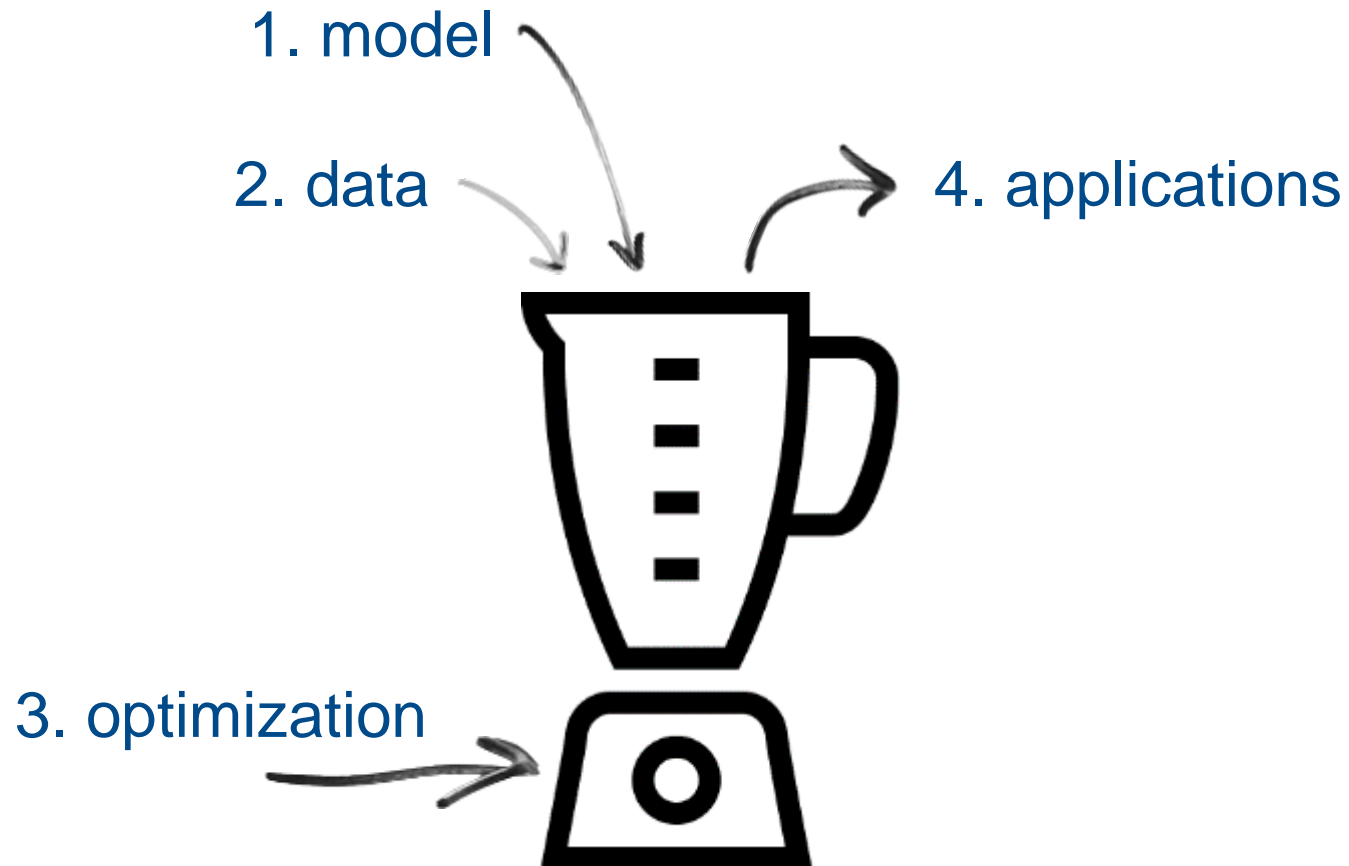
*dynamic model & measurement data*



## Learn model parameters from data

= Tune / optimize model parameters such that simulation output matches measurement data

# Ingredients to Learning



# What System?



System = collector array

- multiple solar thermal collectors connected in series
- multiple rows
- fluid travel time ~5 minutes



# What Model?



- Model used so far („QDT model“, ISO 9806):

$$\dot{Q}_{sp} = F'(\tau\alpha)(K_b G_b + K_d G_d) - a_1(\bar{T} - T_a) - a_2(\bar{T} - T_a)^2 - (mc) \frac{dT}{dt}$$

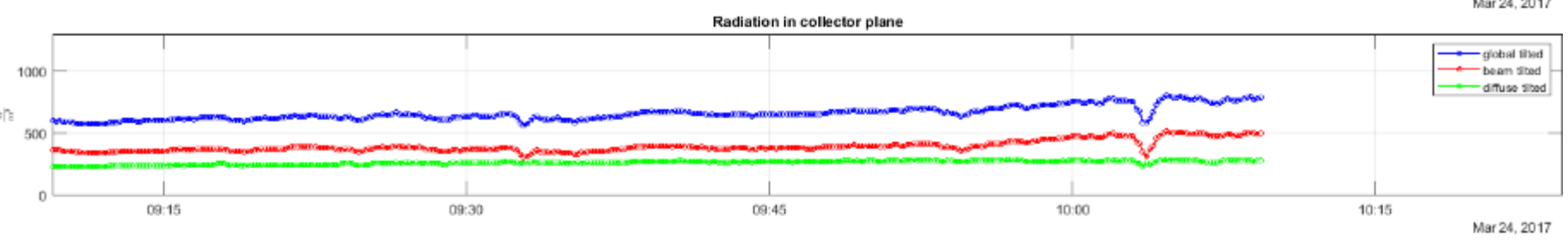
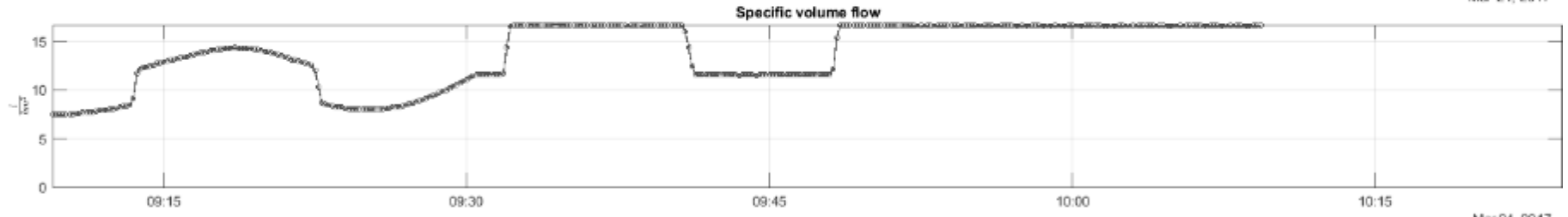
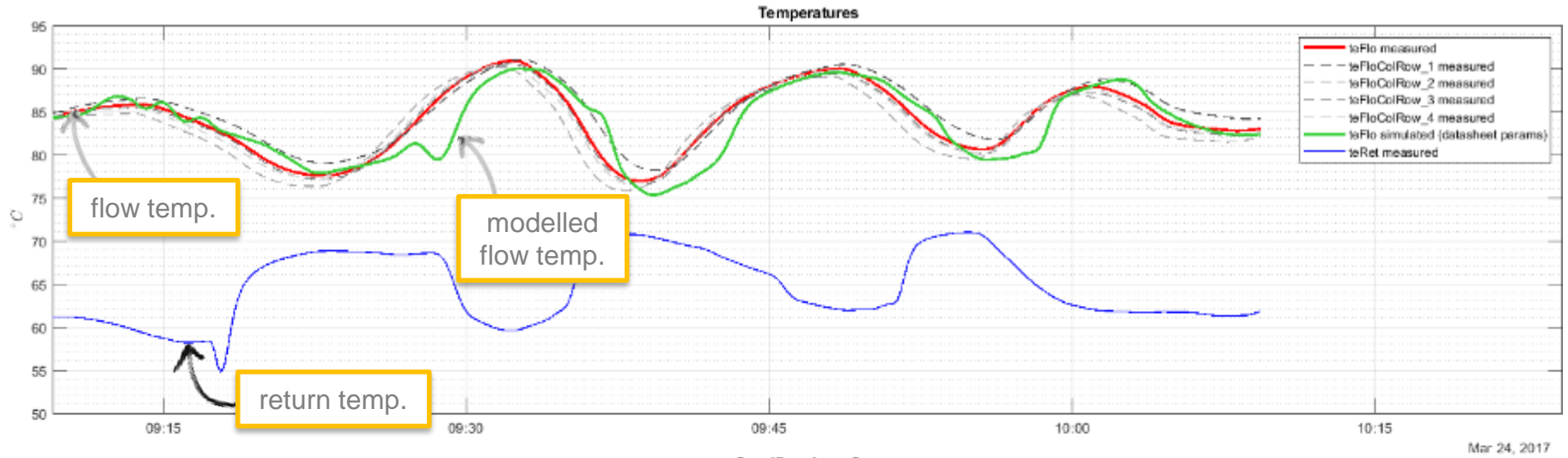
- Simplest extension to collector arrays

$$(mc) \frac{\partial T}{\partial t} = F'(\tau\alpha)(K_b G_b + K_d G_d) - a_1(\bar{T} - T_a) - a_2(\bar{T} - T_a)^2 - \dot{C}_f \frac{\partial T}{\partial x}$$

# System Dynamics

Model: fluid only

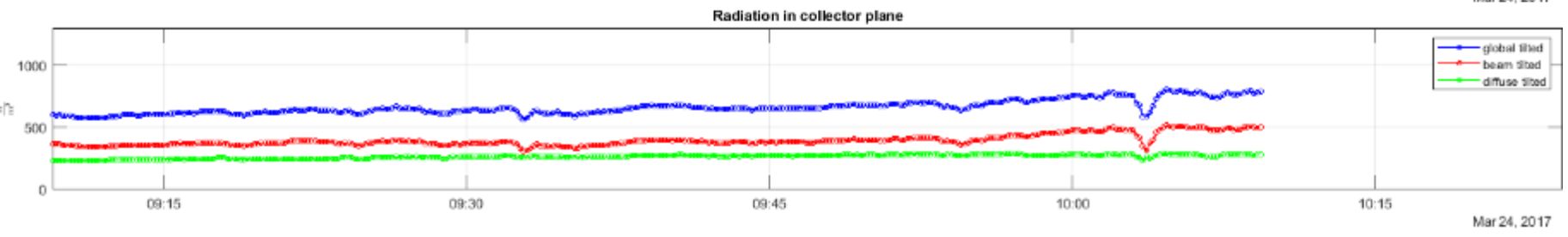
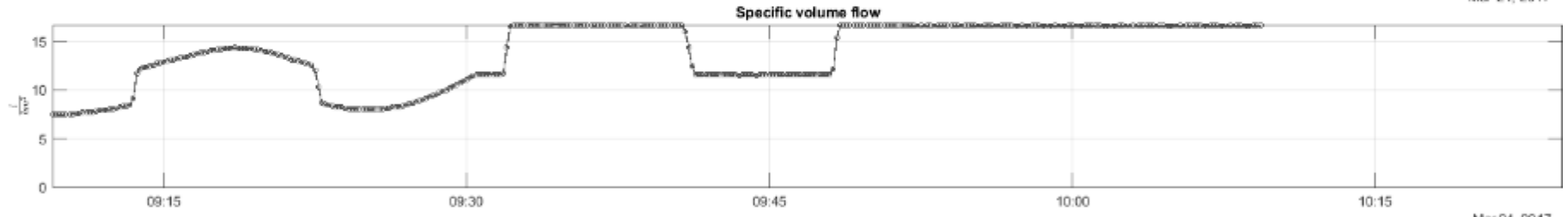
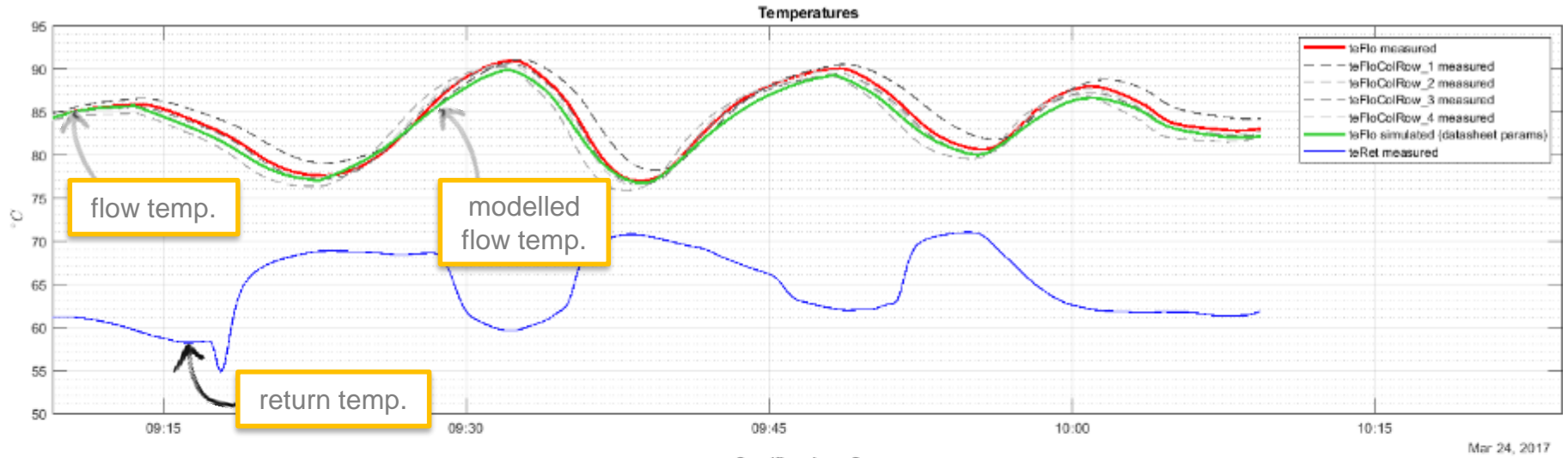
measured vs. simulated outlet temperature collField\_KBB



# System Dynamics

Model: fluid & solid

measured vs. simulated outlet temperature collField\_KBB



# What Model?

- Model used so far („QDT model“, ISO 9806):

$$\dot{Q}_{sp} = F'(\tau\alpha)(K_b G_b + K_d G_d) - a_1(\bar{T} - T_a) - a_2(\bar{T} - T_a)^2 - (mc) \frac{dT}{dt}$$

- Simplest extension to collector arrays: 1-N model

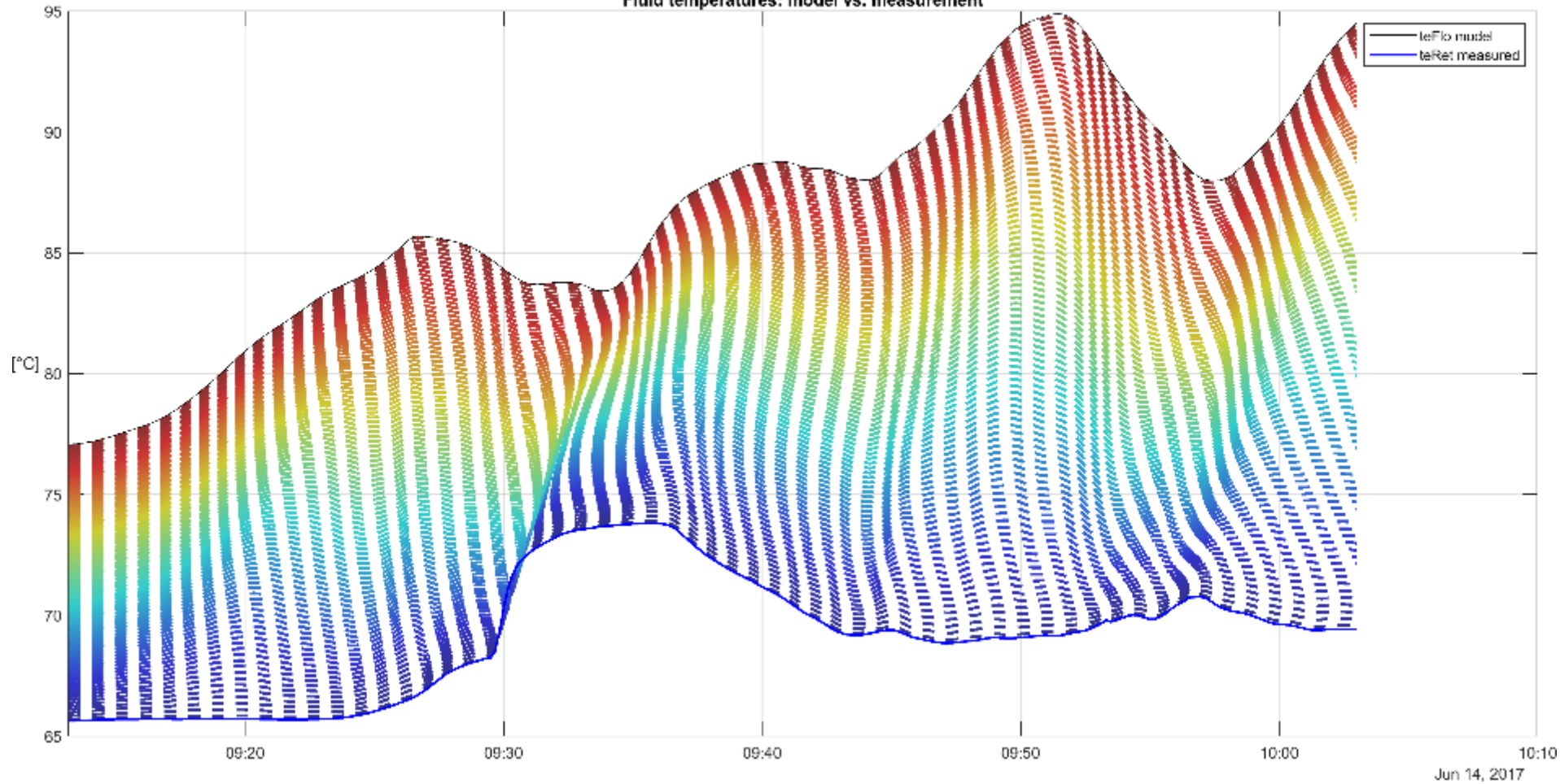
$$(mc) \frac{\partial T}{\partial t} = F'(\tau\alpha) (K_b G_b + K_d G_d) - a_1(\bar{T} - T_a) - a_2(\bar{T} - T_a)^2 - \dot{C}_f \frac{\partial T}{\partial x}$$

- Extension for improved dynamics: fluid & solid model

$$(mc)_m \frac{\partial T_m}{\partial t} = (\tau\alpha)(K_b(\theta)G_b + K_d G_d) - a_1(T_m - T_a) - a_2(T_m - T_a)^2 - D\alpha(T_m - T_f)$$

$$(mc)_f \frac{\partial T_f}{\partial t} = D\alpha(T_m - T_f) - \dot{C}_f \frac{\partial T_f}{\partial x}$$

Fluid temperatures: model vs. measurement



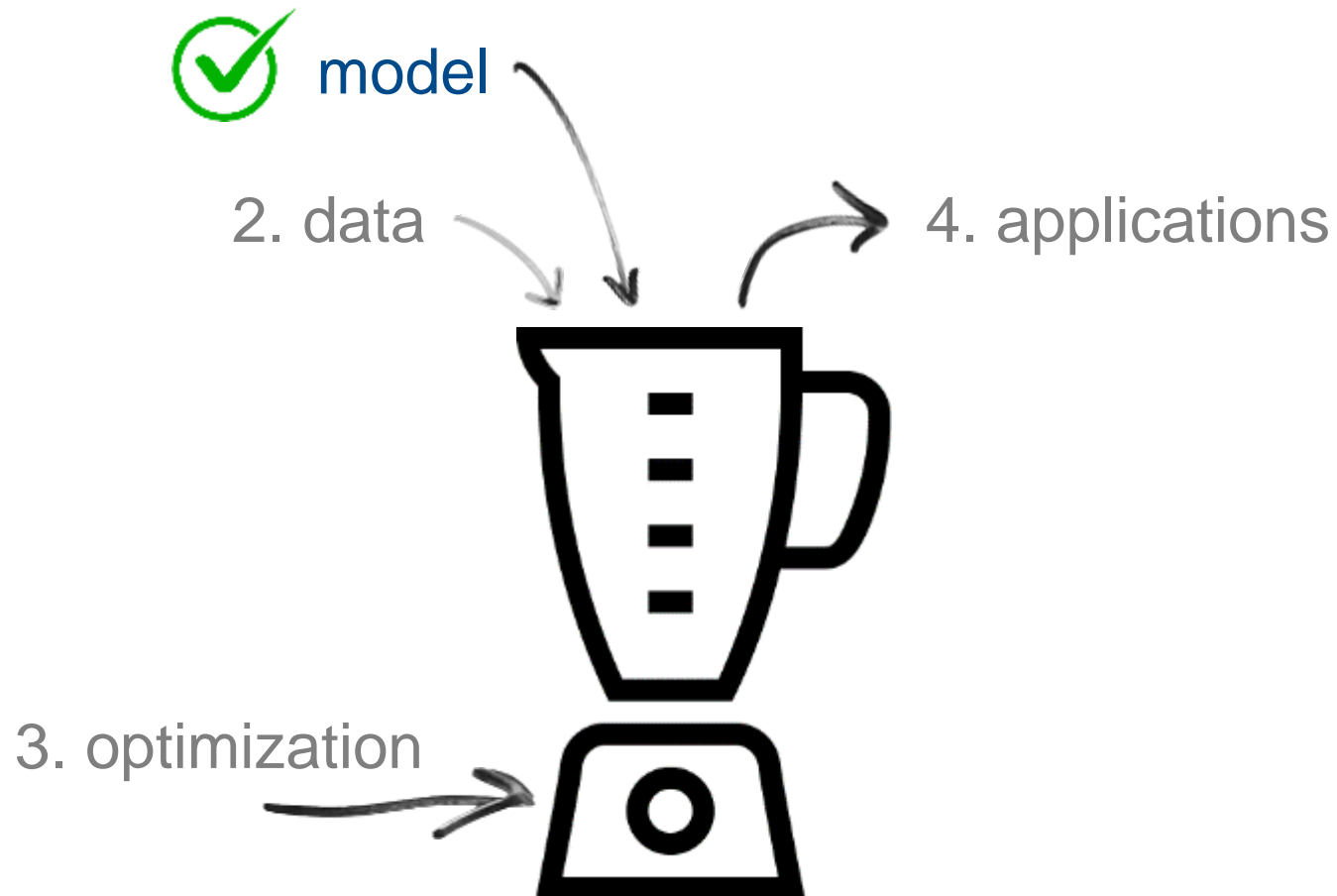
Jun 14, 2017



# Final Model

## Summary

- **Nonlinear coupled PDE model**
- **Parsimonious**
  - **Good enough:** explains data / system dynamics well, low autoregression
  - **Cheap:** only 9 parameters vs. 6
- **Applicable** to a wide range of data
  - **Fully dynamic, accepts a lot of data** → important for estimation process
- **Model properties**
  - Efficient and accurate numeric solution, analytic Jacobians
  - Method of lines / finite volume discretization, stiff ODE solver
  - Nonlinear in states, but linear in parameters
  - Used also for steady-state initialization of simulations
  - Suitable for short- and long-term system predictions

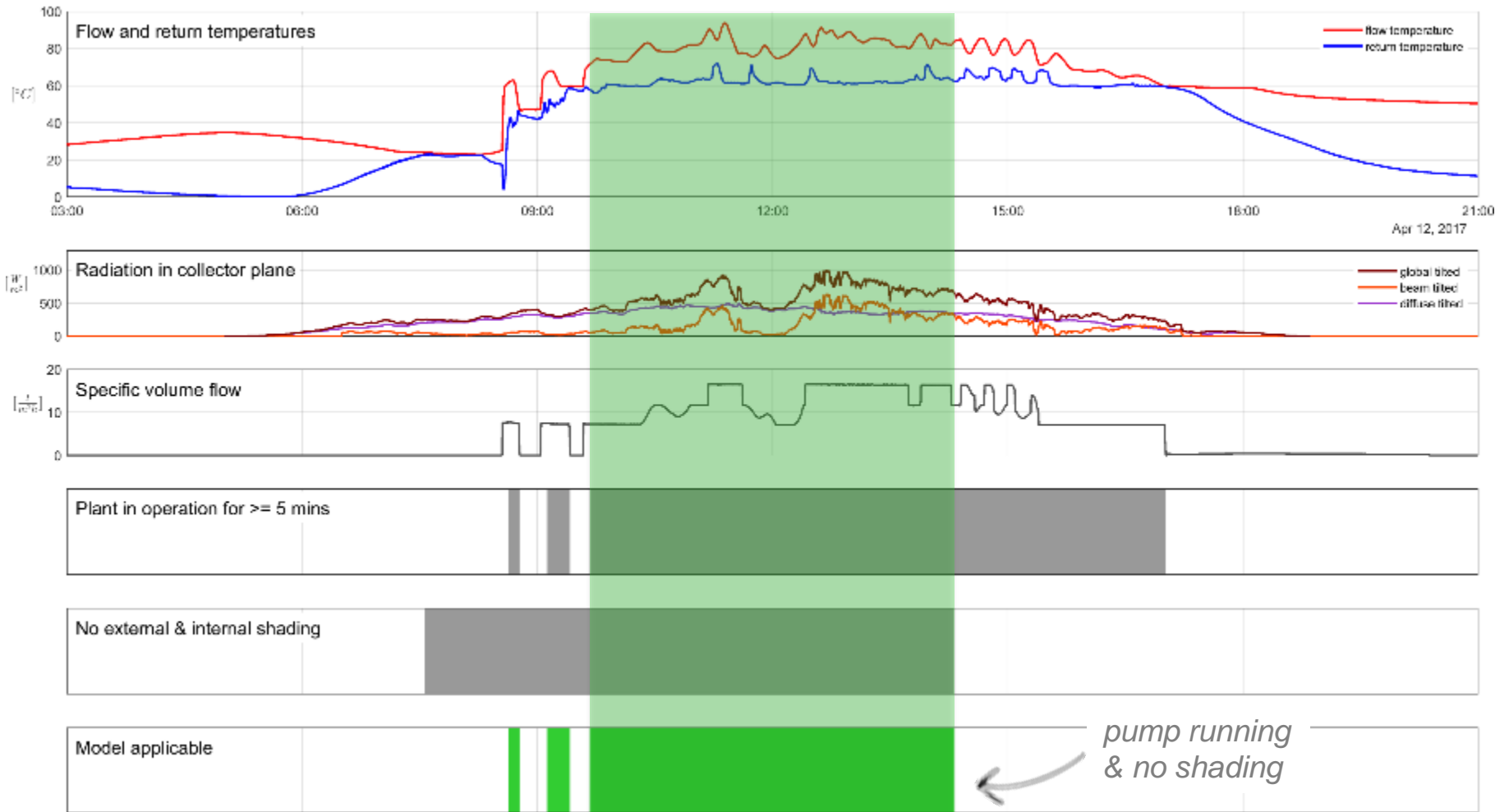


# What Data?



- 6 collector arrays, each  $\sim 500 \text{ m}^2$
- Collector array measurements
  - volume flow
  - inlet & outlet temperature
  - solar radiation (beam & diffuse)
  - ambient temperature
- 1s sampling rate, 10s averages
- $\sim 3$  years of data
- Offline / batch estimation

# Model Validity



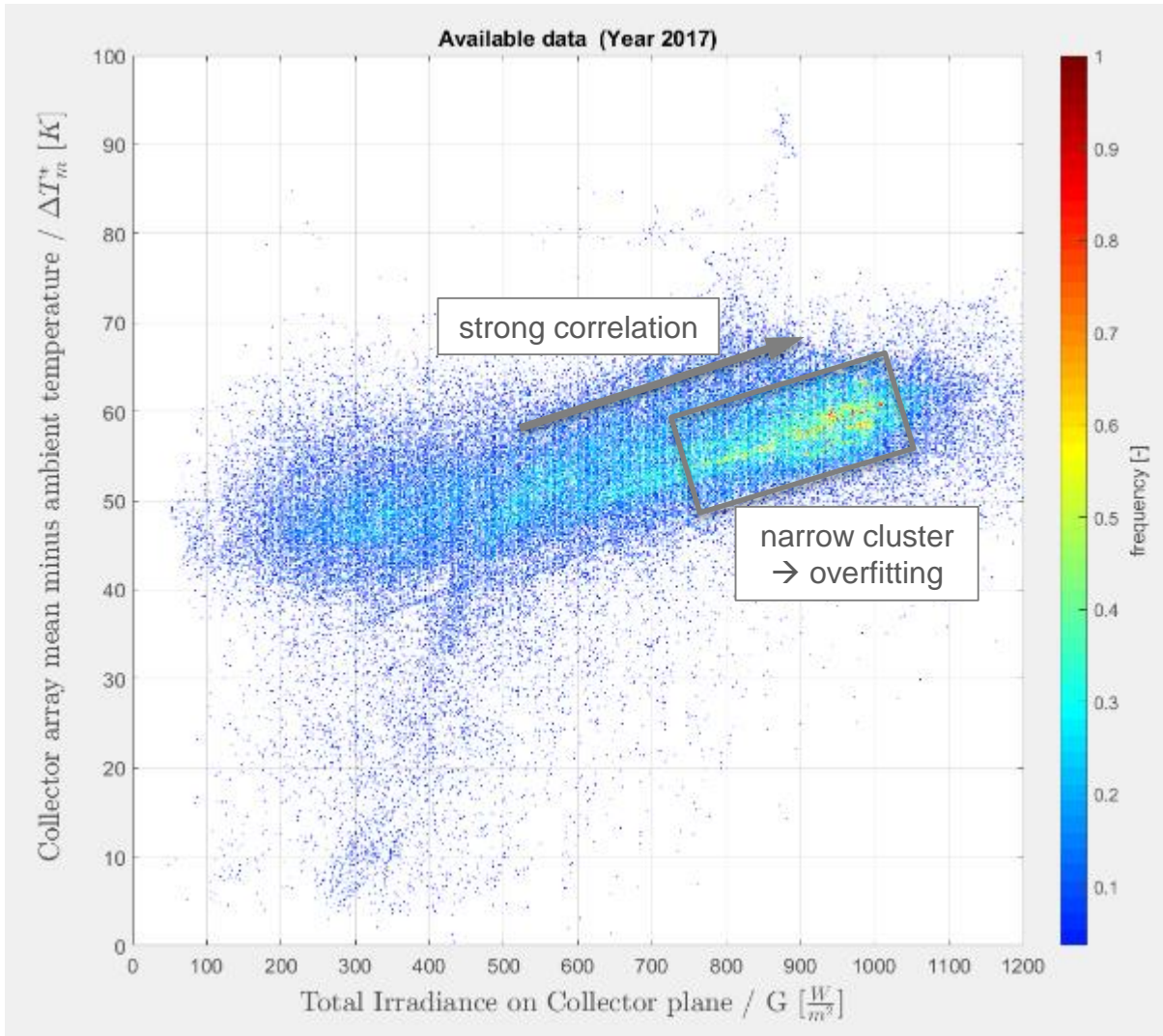
# Data Processing

- Separated chunks of interesting data
  - subdivided into 1-hour intervals
  - ~500 intervals per year
- This data heap is not very helpful for estimation
  - lots of data → **expensive** simulation
  - lots of **similar** data / undesired clustering → overfitting



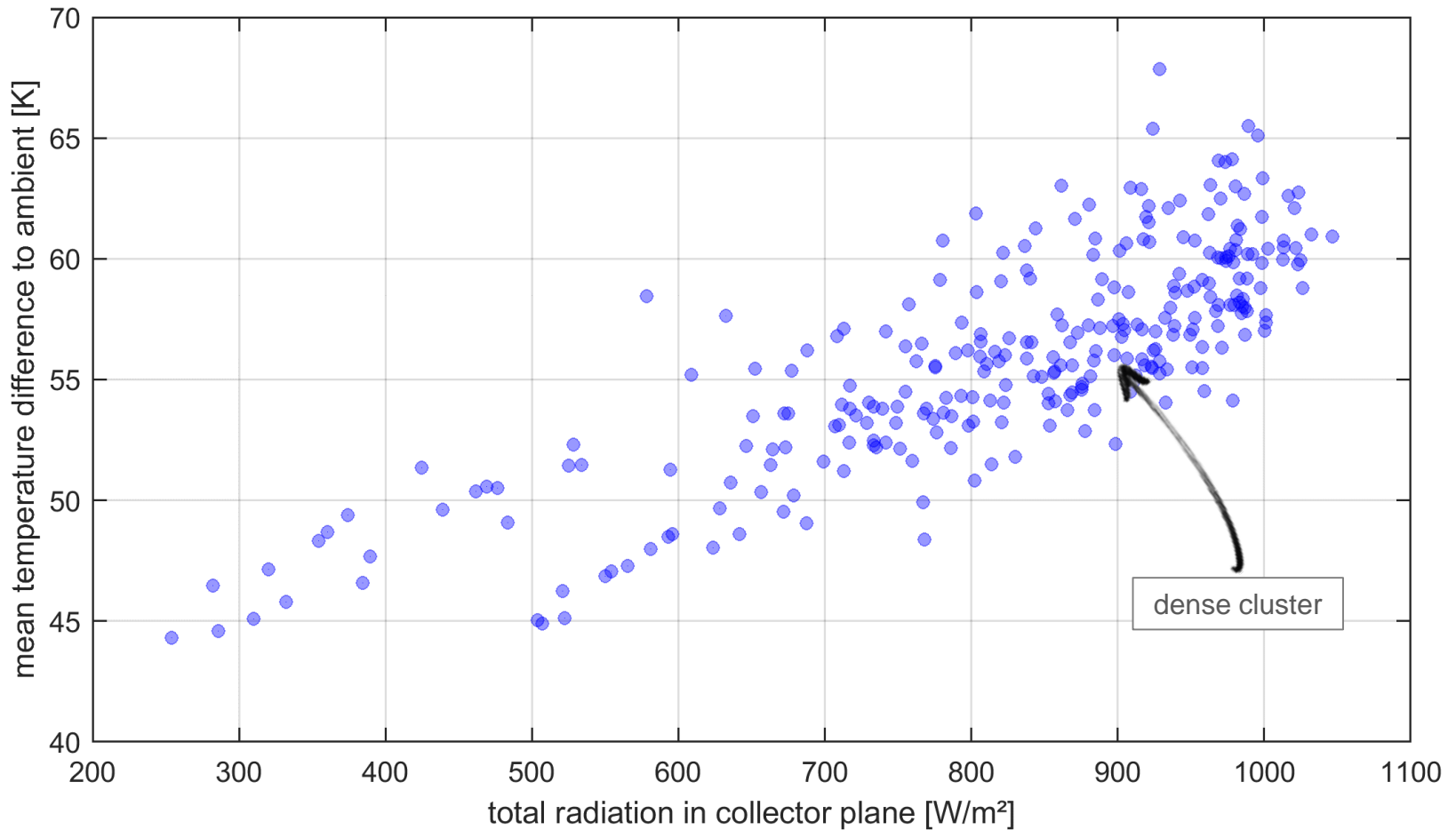
# Clustered Data

2D cut of data



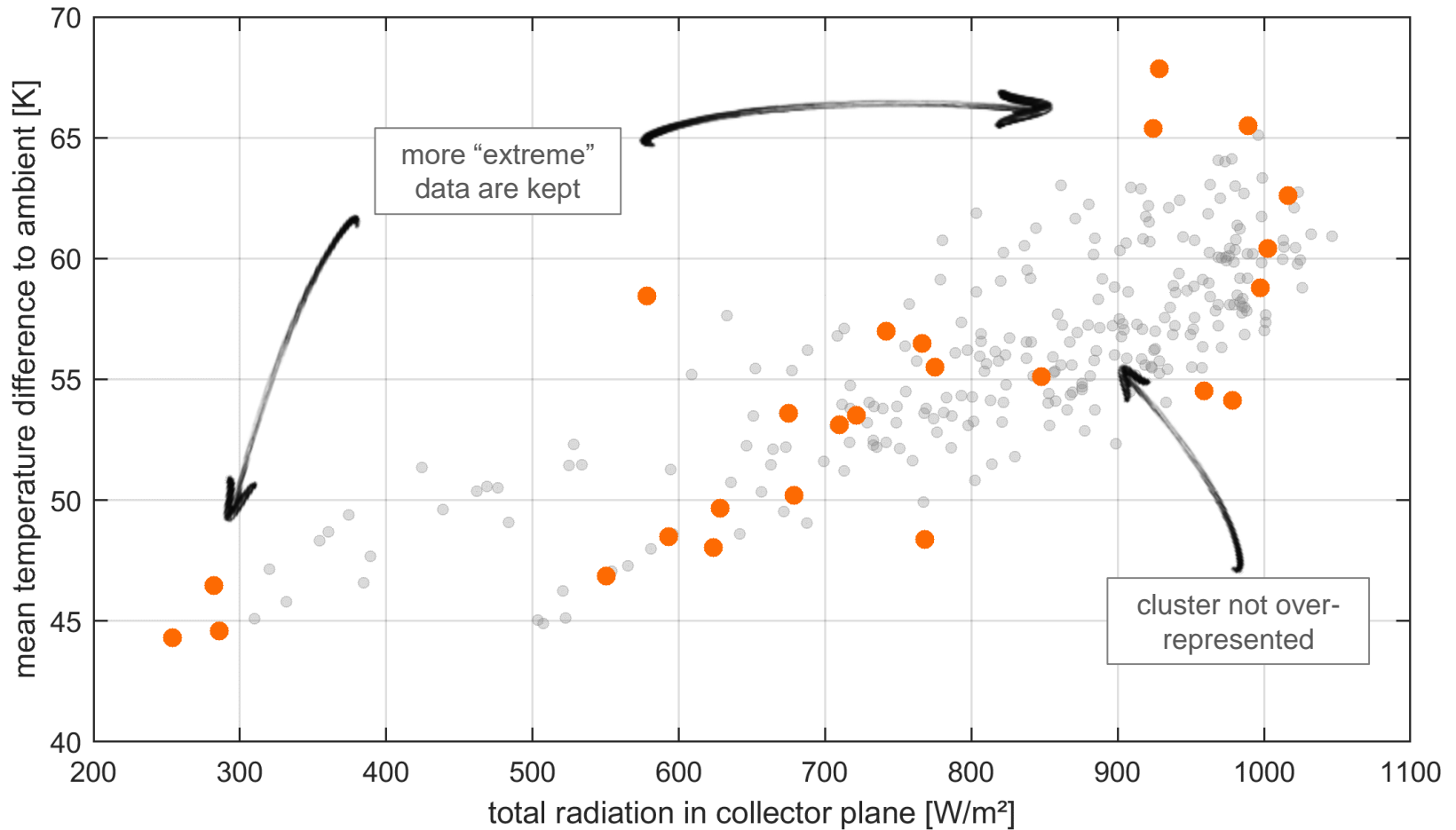
# D-optimal Data Selection

All 1-hour intervals



# D-optimal Data Selection

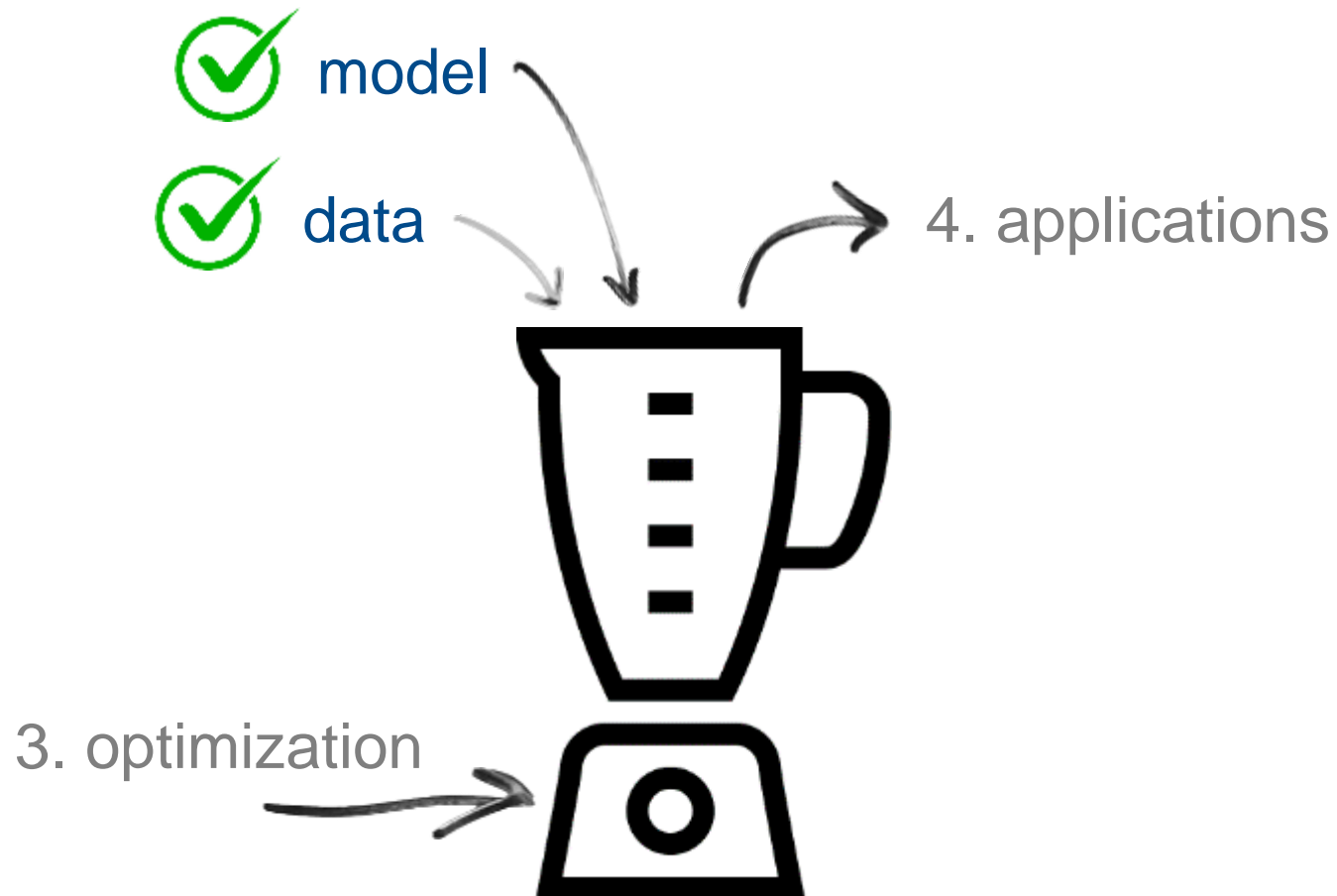
Most informative intervals



- Concept similar to Design of Experiments (DoE)
  - Here data “as-recorded” → optimal data **selection**
  - Fisher information

$$(\mathcal{I}(\theta))_{i,j} = \text{E} \left[ \frac{\partial}{\partial \theta_i} \ln f(X; \theta) \frac{\partial}{\partial \theta_j} \ln f(X; \theta) \right]$$

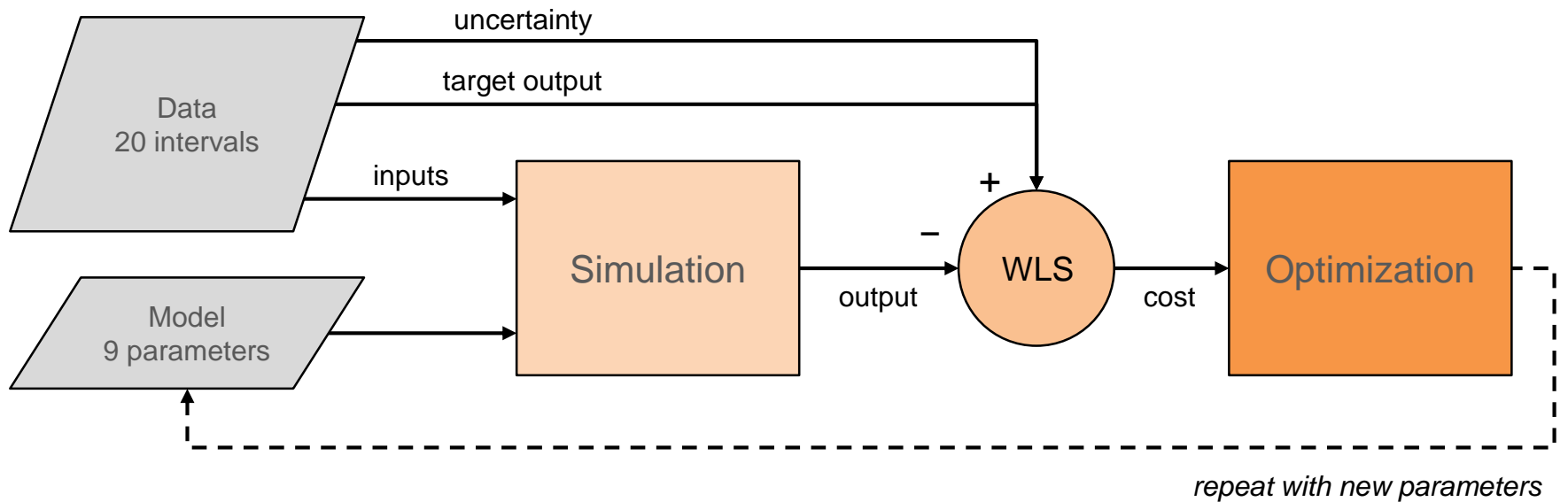
- **D-optimality**
  - Use the **most informative data** for estimation
  - Use data where model is most **sensitive** to parameter changes
- **Advantages**
  - **Automatic optimal data selection**  
Fedorov optimization algorithm: fast, exhaustive optimization
  - **Fast simulation** (only need **~20** out of **~500** intervals)
  - **Good generalization** to new system operating conditions
  - Improves optimization surface





# Estimation Setup

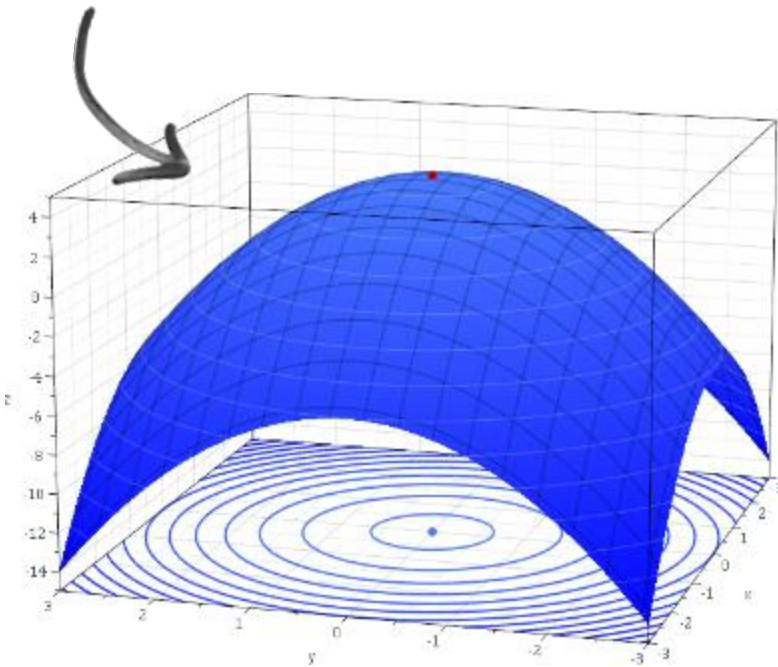
## Single Shooting



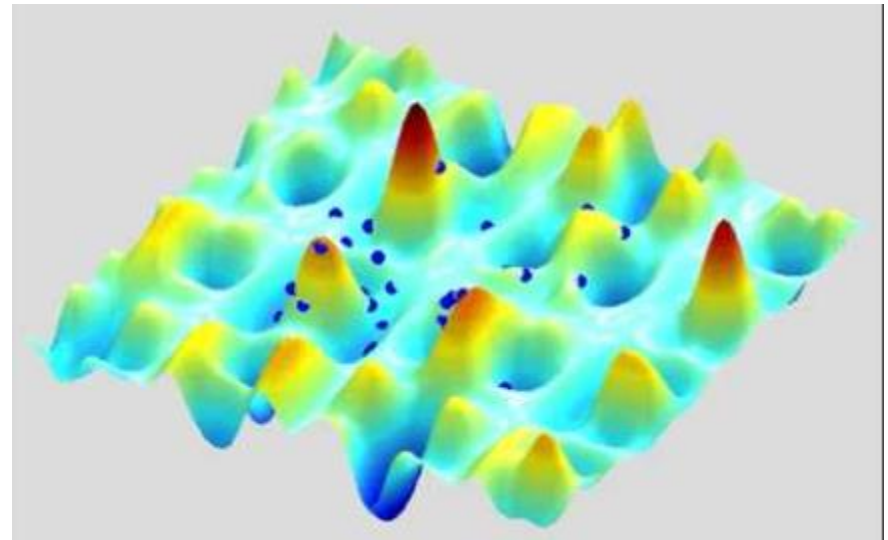
## ■ Nonlinear dynamic optimization

- rough / peaky surface, local minima...

*we'd like to have this  
cost function shape...*

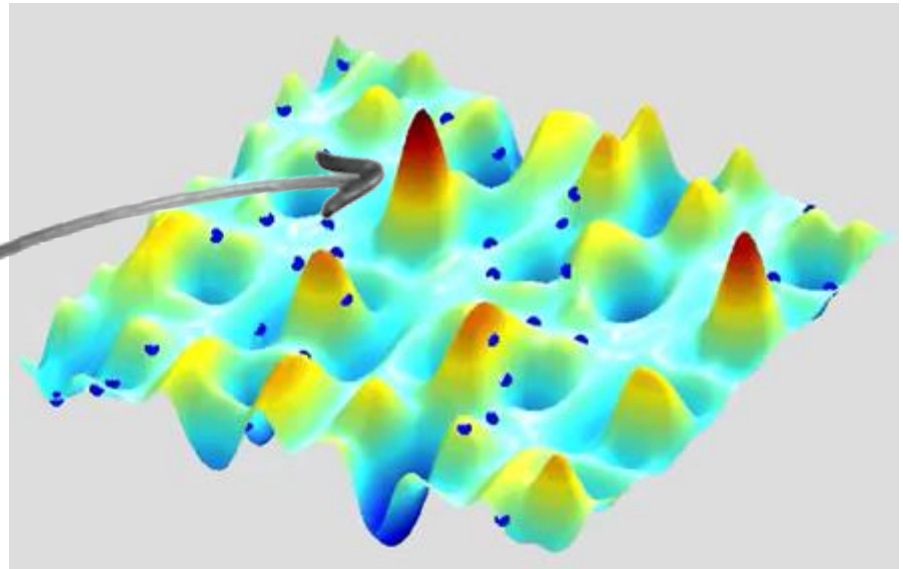


*...but our problem looks  
something like this...*



- **Need stochastic global optimizer**
  - Deterministic algorithms → easily trapped in local minima
  
- **Suitable algorithms e.g.**
  - genetic algorithms
  - simulated annealing
  - differential evolution
  - particle swarm optimization

*optimal data selection  
makes peaks steep & separated*



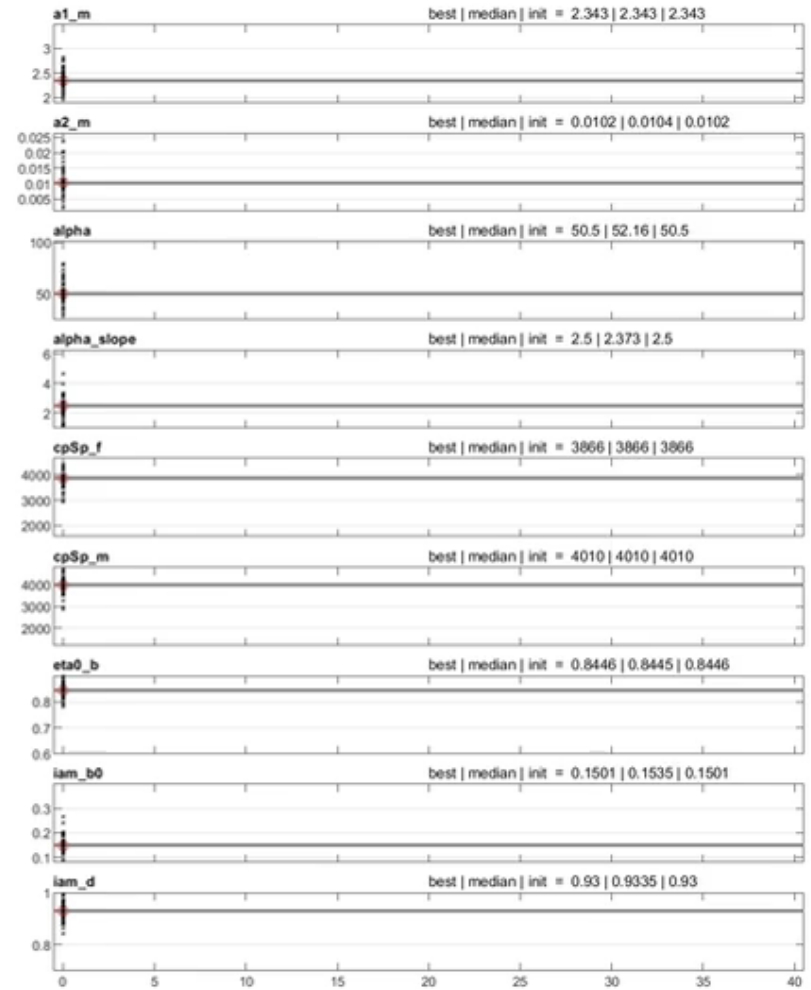
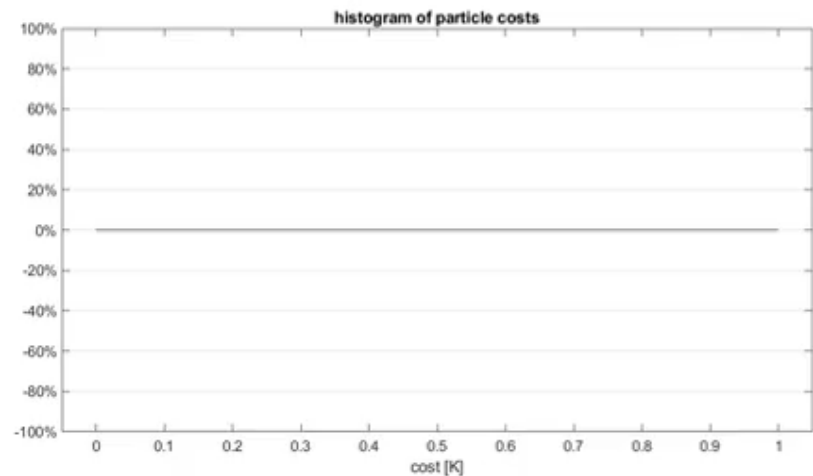
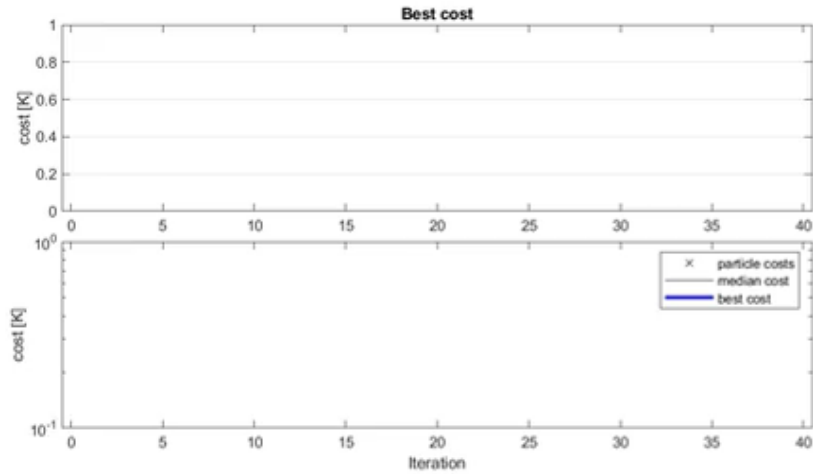
# Static Analysis

Solution used so far



# Optimization Run

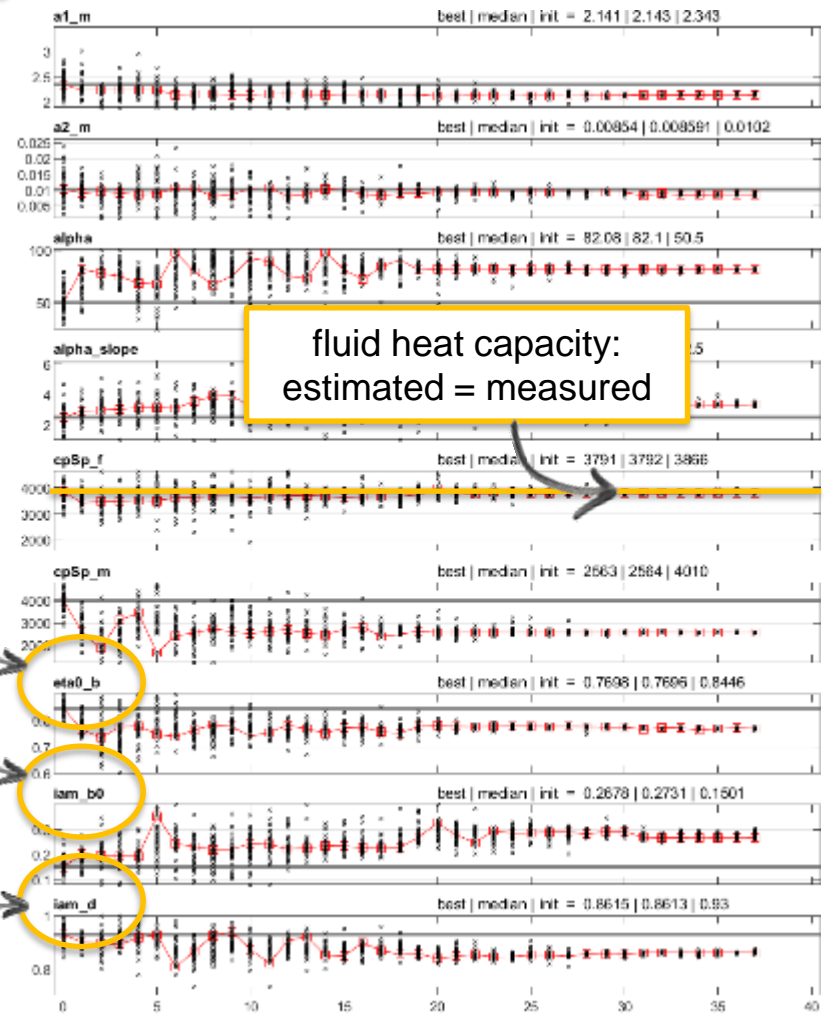
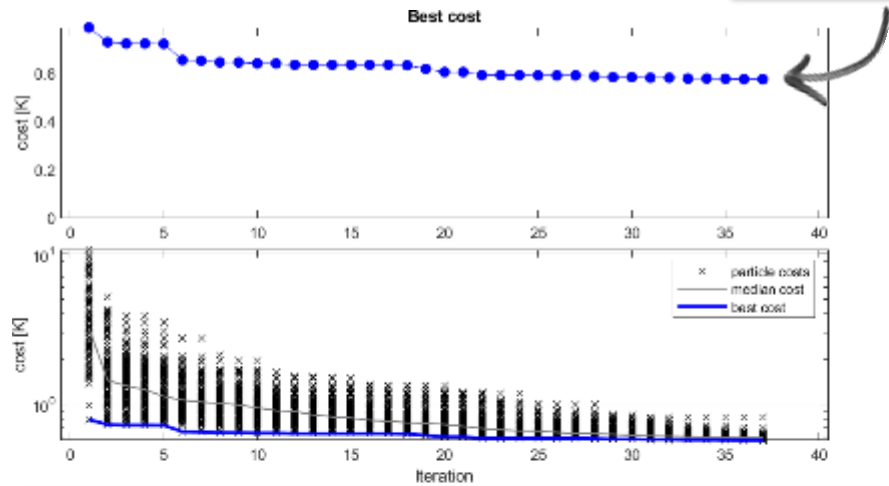
## Particle Swarm





# Parameter Interpretation

RMSE ~ 0.5 K



fluid heat capacity:  
estimated = measured



# Optimization results

## Parameter statistics

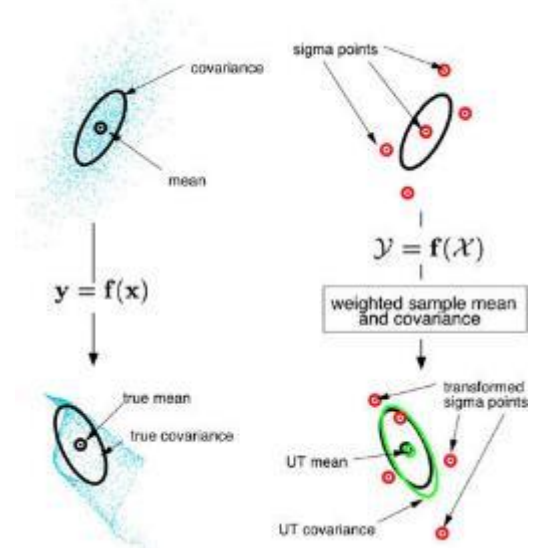
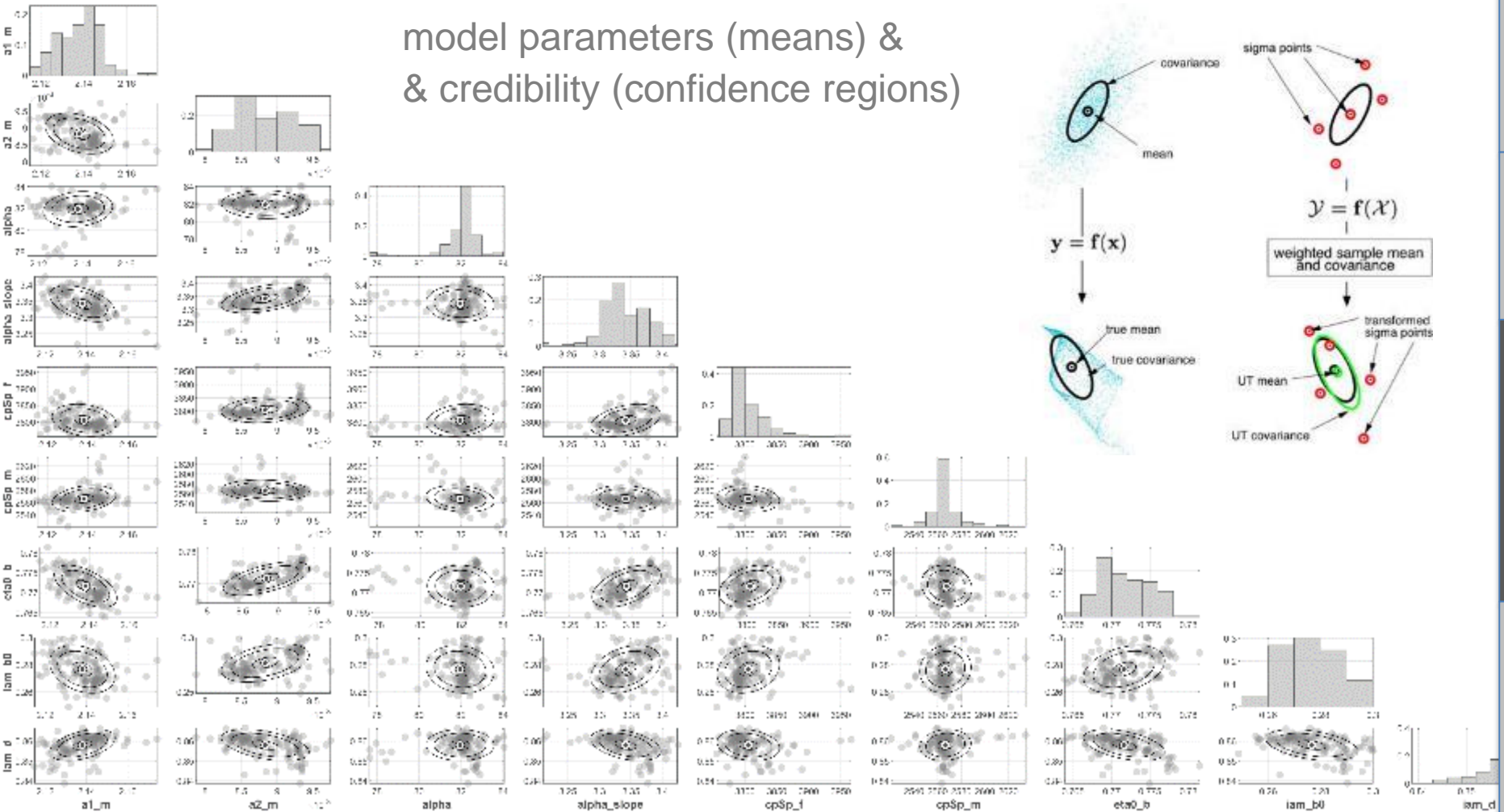
- **Result = model parameters**
  - Parameters have some **uncertainty**
  - parameter noise, model noise, numeric noise
  - sample in param. space → confidence regions (without MCMC)
- **Confidence regions**
  - assuming Gaussian measurement noise
  - we know something about the parameter confidence:
  - parameters are  $F$ -distributed around optimum

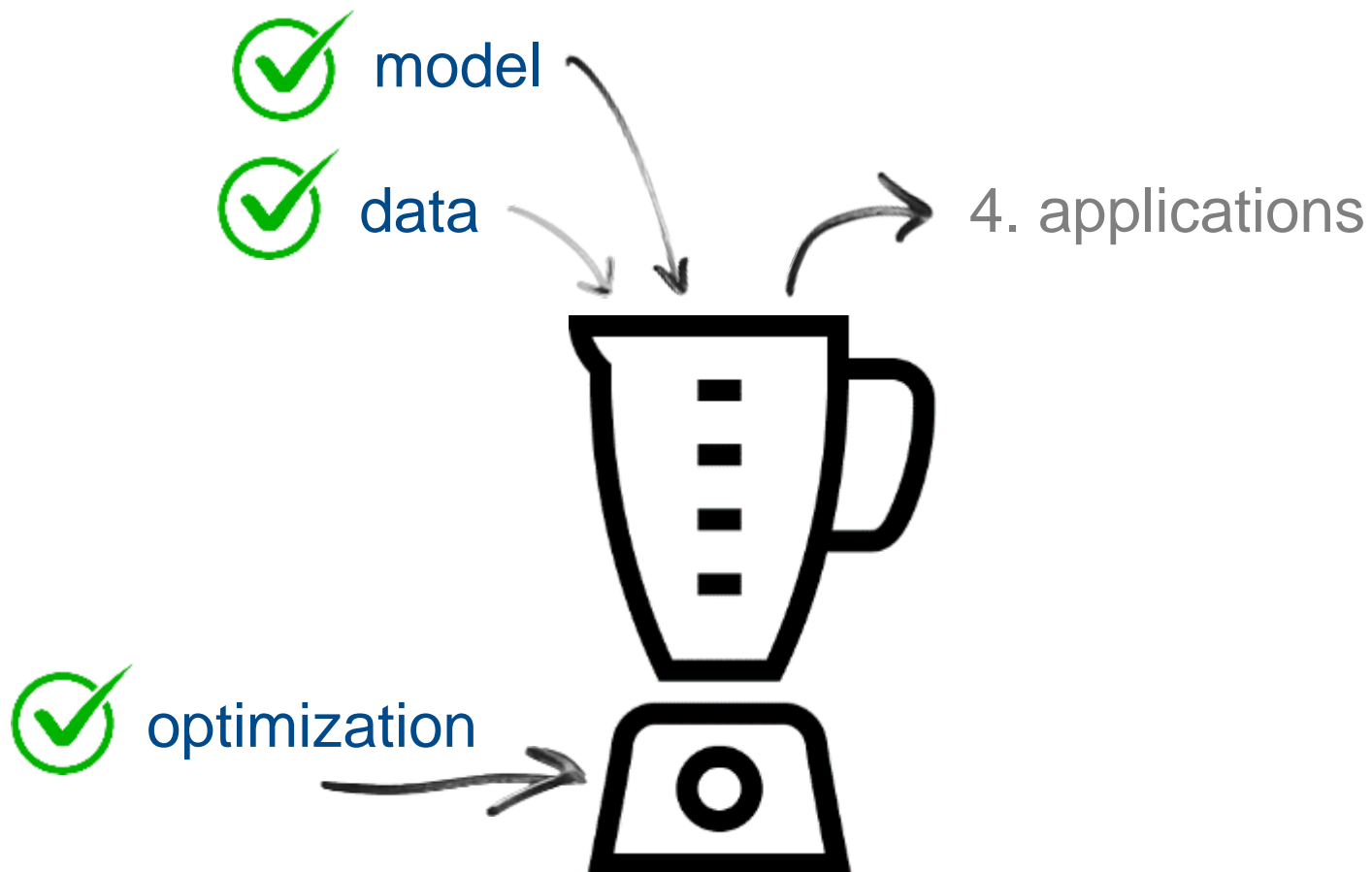
$$J(\theta) = J(\theta_{opt}) \left( 1 + \frac{p}{n-p} F_{p,n-p}^{1-\alpha} \right)$$

# Optimization results

Rich system information

model parameters (means) & credibility (confidence regions)





## 1) Detailed system learning

- “Rich” system description, parameters with physical interpretation
- **Understand** observed system behavior → **increase confidence**

## 2) System surveillance

- E.g. target-actual comparison: system condition vs. datasheet / guaranteed output

## 3) Predictive maintenance

- Periodically repeat test (parallel to normal system operation)
- System KPIs based on parameters, e.g. energy cost  
→ take **timely actions**, make **informed decisions**
- Parameter uncertainty + unscented transform → **quantify prediction uncertainty**

## 4) System control

- Improved system modelling → use calibrated model for MPC

## 5) Test at different locations

- D-CAT allows separation of weather and component effects
- characterization of collector array as technical component
- D-CAT = reproducible, automated test method



An aerial photograph of a modern building complex. The buildings feature large glass facades and are surrounded by a paved courtyard and greenery. A prominent feature is a large array of solar panels mounted on a structure in the foreground. The sky is clear and blue. In the top left corner, there is a yellow vertical bar with a dark blue curved bottom section containing the text 'AEE INTEC'. Below this, a white horizontal bar contains the text 'IDEA TO ACTION'.

**AEE INTEC**

**IDEA TO ACTION**

**Danke für Ihre  
Aufmerksamkeit**